# Deep Learning Techniques for Music Generation 2. Introduction to Deep Learning

Jean-Pierre Briot

Jean-Pierre.Briot@lip6.fr

Laboratoire d'Informatique de Paris 6 (LIP6)
Sorbonne Université – CNRS



Programa de Pós-Graduação em Informática (PPGI)
UNIRIO

# **Deep Learning**

#### **Deep Learning – Already There**

Translation, ex: Google Translate



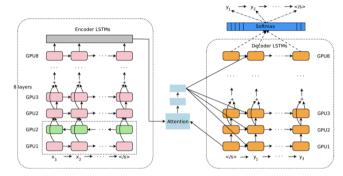
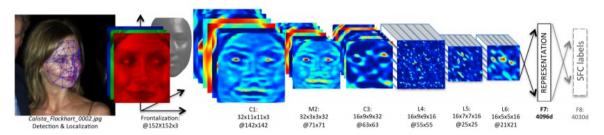


Image Recognition, ex: Facebook

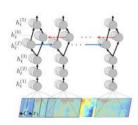


Speech Recognition, ex: Apple Siri, Amazon Echo...



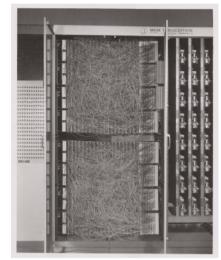




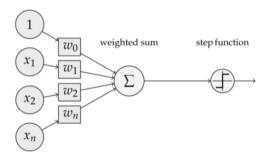


# **History**

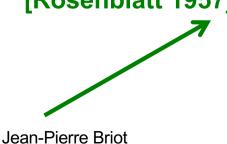
# History: From Perceptron to Artificial Neural Networks to Deep Learning (1/4)

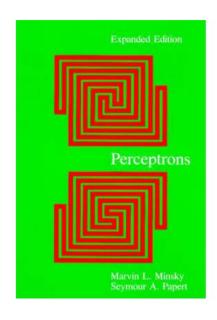


inputs weights

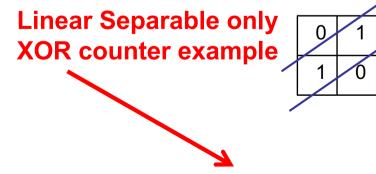


Perceptron [Rosenblatt 1957]

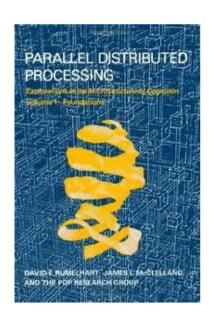




Perceptrons (Book)
[Minsky & Papert 1969]



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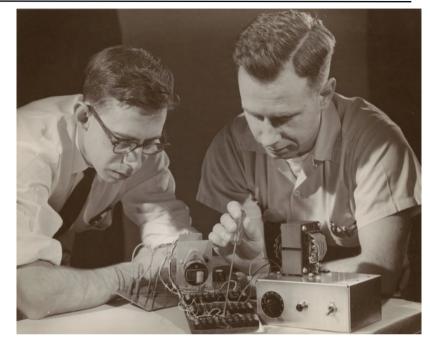
PDP (Books) [Rumelhart et al. 1986]

Multi-layer networks Backpropagation

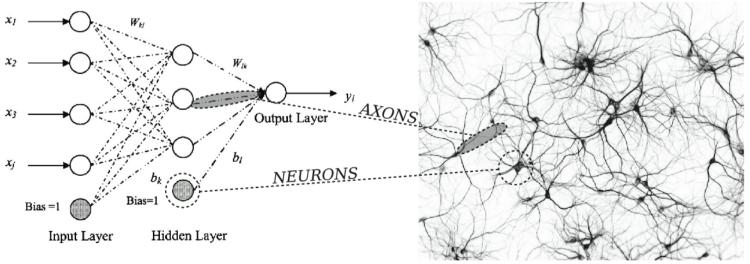


## Deep Learning Bio-inspired or/and Regression-based?

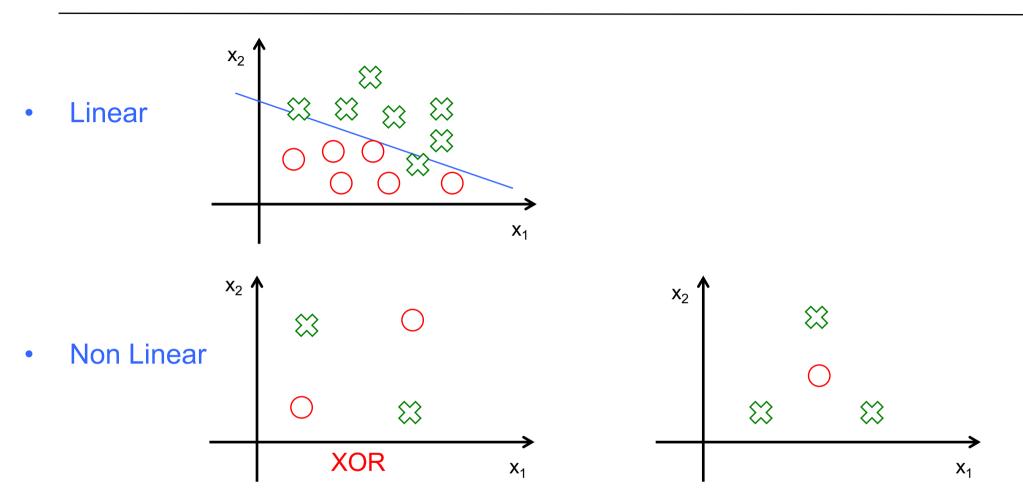
- Historically Perceptron bioinspired
- Aimed at Character Recognition



#### NEURAL NETWORK MAPPING

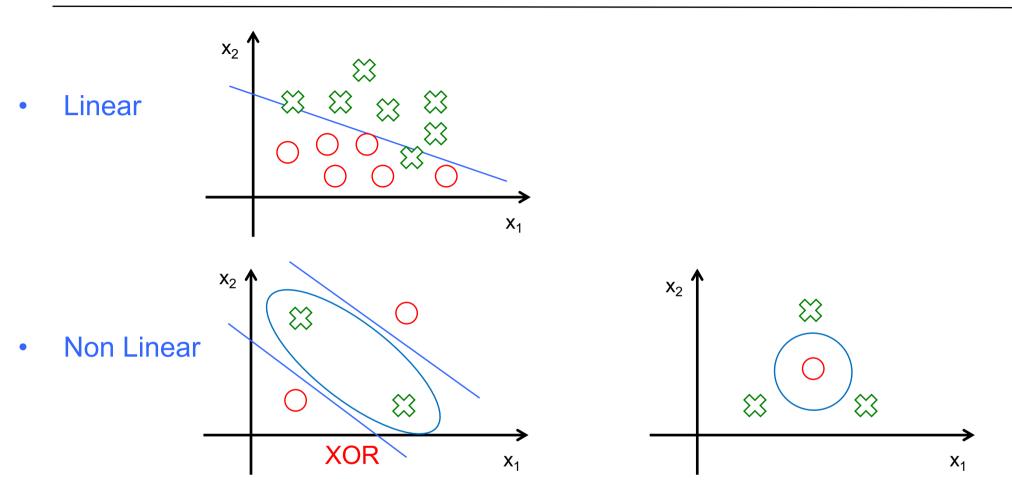


#### **Linear vs Non Linear Decision Boundary**



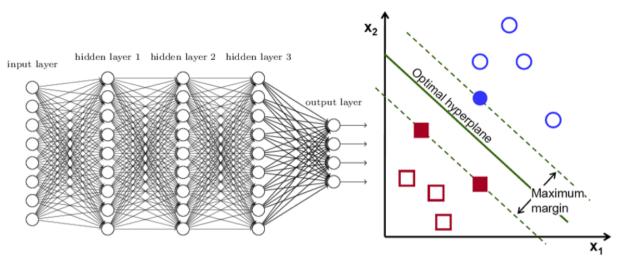
- Argument (XOR) used by [Minsky & Papert 1969] to criticize Perceptrons [Rosenblatt 1957] (and advocate Symbolic Artificial Intelligence)
- This stopped research on Perceptrons/Neural Networks for a long while
- until Hidden Layers and Backpropagation or/and Kernel Trick (see later)
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#### **Linear vs Non Linear Decision Boundary**



- Argument (XOR) used by [Minsky & Papert 1969] to criticize Perceptrons [Rosenblatt 1957] (and advocate Symbolic Artificial Intelligence)
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# History: From Perceptron to Artificial Neural Networks to Deep Learning (2/4)



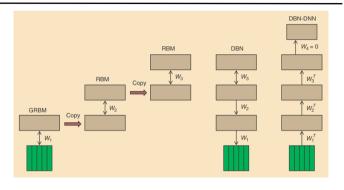
Difficulty to Efficiently Train Networks with many Layers

SVM [Vapnik 1963] SVM + Kernel Trick [Vapnik et al. 1992]

**Unstable Gradients** 

Nice Model and Optimized Implementation

**Margin Optimization** 



Pre-Training [Hinton et al. 2006]
Layer-Wise Self-Supervised
Training/Initialization

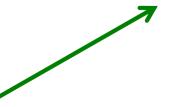
Rank	Name	Error rate	Description
1	U. Toronto	0.15315	Deep learning
2	U. Tokyo	0.26172	Hand-crafted
3	U. Oxford	0.26979	features and learning models. Bottleneck.
4	Xerox/INRIA	0.27058	

ImageNet 2012 Image Recognition Challenge Breakthrough

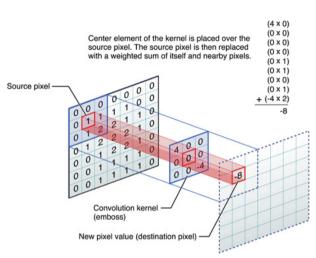


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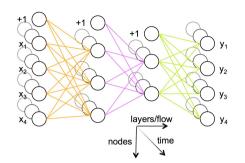
# History: From Perceptron to Artificial Neural Networks to Deep Learning (3/4)



Convolutional Networks

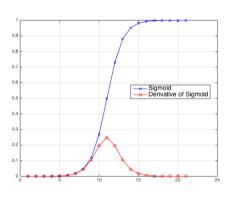
Equivariance (to translation) & Invariance (to small transformations)

[Le Cun et al. 1998]



Recurrent Neural Networks (RNN) (1986)

**Temporal Invariance** 



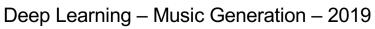
**Gradient Vanishing** or Explosion (1991)

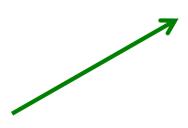


Long Short-Term Memory (LSTM) [Hochreiter & Schmidhüber 1997]



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# History: From Perceptron to Artificial Neural Networks to Deep Learning (4/4)



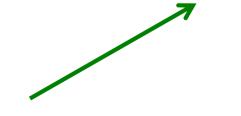
Massive Data
Available



Efficient Implementation Platforms



Affordable Efficient Parallel Processing (Graphic Cards)



# What and Why

#### **Deep Learning**

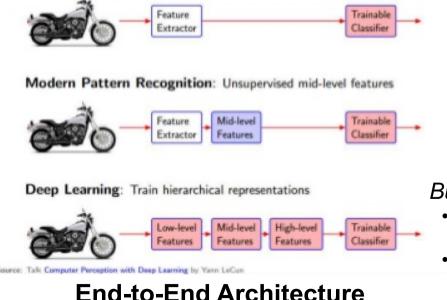
- Many Hiddden Layers
  - Deep Architecture
  - Deep Representation
- Various Types
  - Supervised learning
  - Unsupervised learning
  - Recurrent networks
  - Stochastic Neurons (ex: Restricted Boltzmann Machines)
- Various Objectives
  - Classification
  - Prediction
  - Feature extraction
  - Generation
    - » Related Content (ex: Melody Accompaniment)
    - » New Content (ex: new Melody)
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#### Why Deep?

- More Complex Models
- Learns better Complex Functions
- Hierarchical Features/Abstractions
- No Need for Handcrafted Features

Traditional Pattern Recognition: Fixed/Handcrafted feature extraction

(Automatically Extracted)





### **Distributed Representations**

But the choice of the input representation is important

- Ex: for Audio:
  - Waveform or Spectrum
- Ex: For Symbolic representation
  - Additional information, ex: beat, fermata, enharmony (Cb =/= B)

#### Ex. of Handcrafted Features – Bag of Features [Brendel, 2019]

- Bag of Features (BoF) Model
- Define key Visual Features
  - Ex: Human eye, Feather





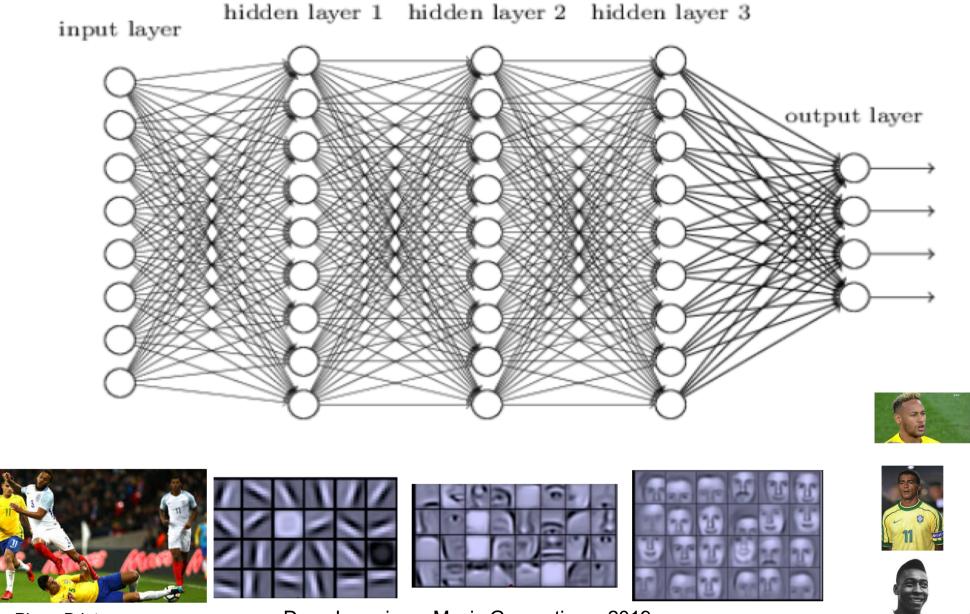
Count how often each Feature is Present in the Image





- Classify based on these Numbers
  - Human: Eye = 2
  - Bird: Feather = 18

#### **Successive Features/Abstractions Constructed**



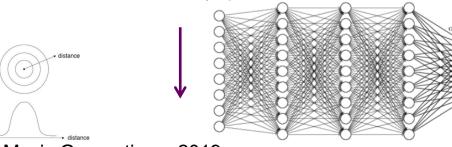
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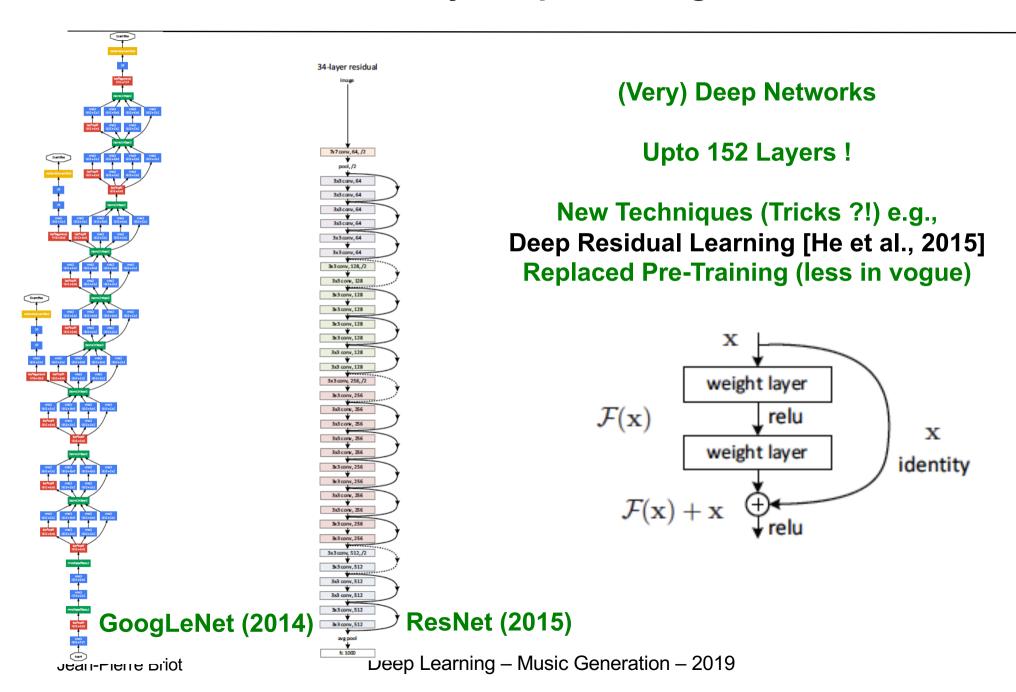
#### Why Deep?

- Need for Deep ?! [Ba & Caruana 2014]
  - Train a Shallow Net to Mimic a Deep Net
  - Mimic = Train on the Logits (predicted values, before softmax/probabilities),
     not on the Original Output Data
  - Equivalent Accuracy
  - But for Convolutional Nets, Mimic Net Does Not Match the Initial Accuracy!
     [Urban et al.& Caruna 2016]
- Counter Argument (Theorem) [Eldan & Shamir 2016]
  - There is a simple radial function on R<sup>d</sup>, expressible by a 3-layer net, but which cannot be approximated by any 2-layer net to more than a constant accuracy unless its width is exponential on the dimension d
  - Depth → vs/and Width |

Radial function = Function whose value at each point adepends only on distance between point and origin



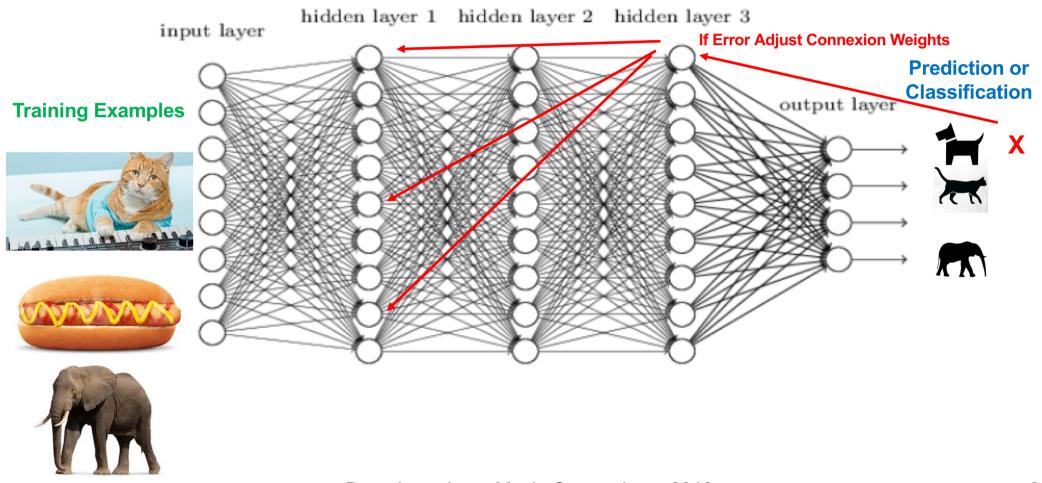
#### **Very Deep Learning**



# **Linear Regression and Neural Networks**

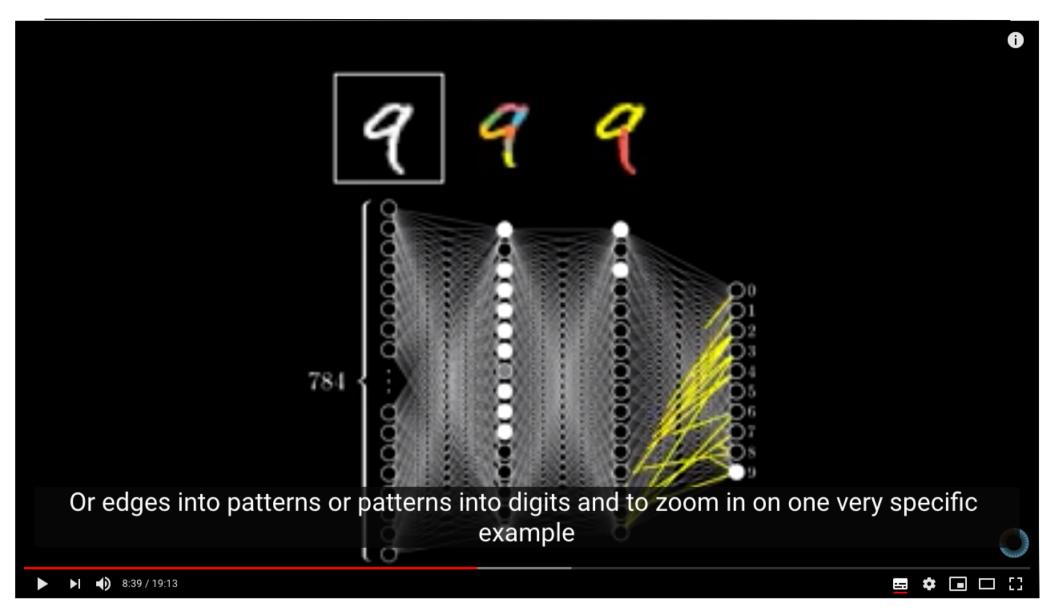
#### **Neural Networks in One Slide**

#### Principle – Error Prediction/Classification Feedback



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### **Nice Animation [3Blue1Brown]**



#### **Machine Learning**

- Why learning?
- What is machine learning?
- A computer program is said to learn from experience E with respect to some class of tasks T and performance measure P, if its performance at tasks in T, as measured by P, improves with experience E [Mitchell, 1997]

#### **Machine Learning Typology**

- Learning = Using Experience/Memory to Infer Information/Behavior and to Improve Decision/Action
- Dynamicity
  - Off-Line (Training Phase vs Using/Production Phase)
    - » Ex: Supervised Learning
      - But also Incremental versions
  - On-Line/Incremental
    - » Ex: Reinforcement Learning
      - But also Off-line versions (ex: Deep Reinforcement Learning Replay Mechanism)
- Provided Information
  - Supervised (Correct Output)
  - Unsupervised (Ø)
  - Reward-Based (Quality assessment)

## **Machine Learning Typology (2)**

#### Data/Statistics-oriented

- Supervised and Off-Line (mostly)
  - » Neural Networks
  - » Deep Networks
  - » Support Vector Machines
  - » Bayesian Networks
- Unsupervised
  - » Clustering (ex: k-Means)
  - » Principal Component Analysis (PCA)
  - » Autoencoders
  - » Deep Networks

#### Decision/Action-oriented

- Fitness/Reward-based
  - » Evolutionary Algorithms
  - » Reinforcement Learning

#### Knowledge/Rules-oriented

- » Memory-based Reasoning and Case-Based Reasoning
- » Inductive Logic Programming (ILP)

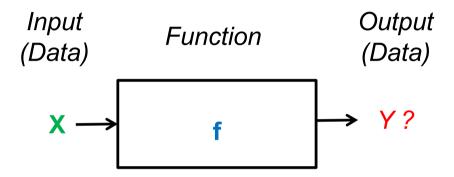
#### Machine Learning and Artificial Intelligence

Machine Learning is Part of Artificial Intelligence Techniques
 But also:

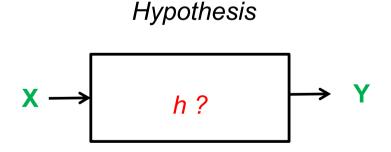
- Reasoning
- Planning
- Knowledge Representation
- User Modeling and Interaction
- Collaboration (Multi-Agent Systems)
- Natural Language Processing
- Dialogue
- Speech Processing
- Decision
- Game Theory
- Optimization
- Robotics

#### Machine Learning (Data Oriented/Supervised Learning)

Traditional Programming



Machine Learning (Supervised Learning)



Function/Module Configuration

(Pre-Existing Representation Model)

#### **Machine Learning (Data Oriented)**

3 Components [Domingos 2015]:

#### Representation

- To Model Predictors/Classifiers
- e.g., Decision Tree, Rule, Neural Network, Graphical Model...

#### Evaluation

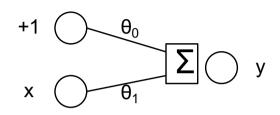
- of Predictors/Classifiers (Accuracy)
- Cost, e.g., Squared Error, cross-entropy...
- Precision, Recall

#### Optimization

- To Search among Predictors/Classifiers,
- e.g., Batch Gradient Descent, Greedy Search, Stochastic Gradient...

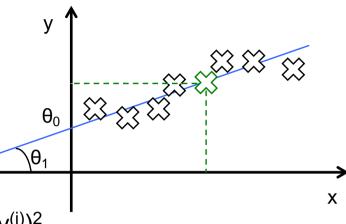
# (Simple) Linear Regression (Prediction)

Representation



Model (Hypothesis)

$$h(x) = \theta_0 + \theta_1 x$$



Evaluation

Cost function : 
$$J(\theta_0, \theta_1) = J_{\theta} = 1/2 \text{*m}_{i=1}^{m} \sum_{j=1}^{m} (h(x^{(j)}) - y^{(j)})^2$$

Optimization (Training)

Distance between predicted and real

Objective: Find out "best" values of  $\theta_0$  and  $\theta_1$  to minimize Cost function  $J_{\theta}$ 

with:

$$Example^{(1)}\ Example^{(2)}$$

Input Dataset: X:

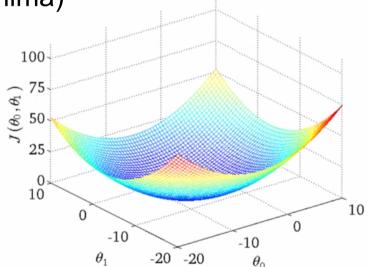
and Output Dataset: y:

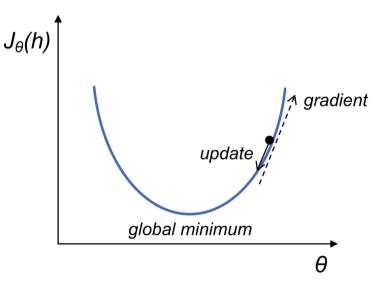
## **Optimization**

- Objective: Minimization of Cost function J<sub>θ</sub>
- Usual/simple algorithm: Gradient descent
- Therefore, we need to compute the Cost, but also the Gradients (partial derivatives respective to each θ (weight)) in order to guide gradient descent

As this Cost function is convex, there is a global minimum (and no local

minima)





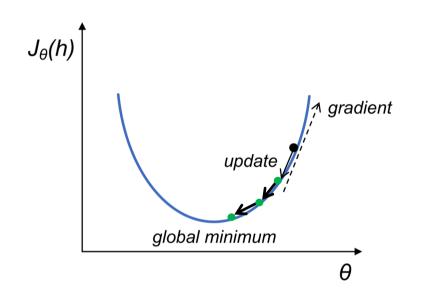
## Learning rate and Stochastic Gradient Descent (SGD)

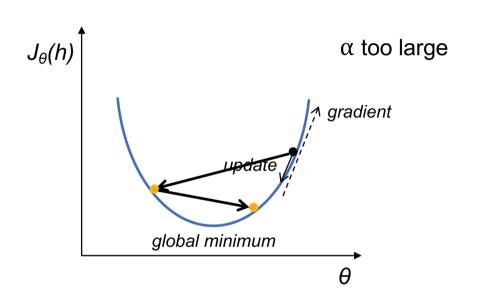
**Update Rule** 

$$\theta_0 := \theta_0 - \alpha \, dJ(\theta_0, \theta_1)/d\theta_0$$
  
 $\theta_1 := \theta_1 - \alpha \, dJ(\theta_0, \theta_1)/d\theta_1$ 

$$\theta_1 := \theta_1 - \alpha \, dJ(\theta_0, \theta_1)/d\theta_1$$

 $\alpha$ : Learning rate





**Compute Cost and Gradients** 

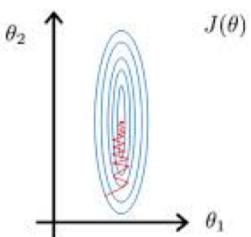
Gradient Descent (SGD): for ALL examples

Stochastic Gradient Descent (SGD): for ONE example (randomly chosen)

for a Batch (subset) randomly chosen MiniBatch:

## **Scaling and Mean Normalization**

To improve learning convergence (faster), better to have features  $(x_1, x_2...)$  on a similar scale



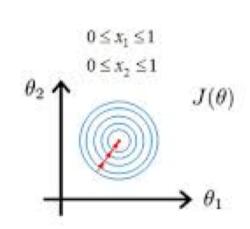
x := x / range(x)

**Feature Scaling** 

(Could also apply)

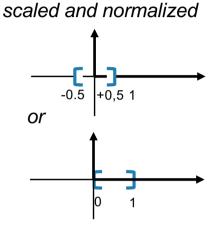
Mean Normalization

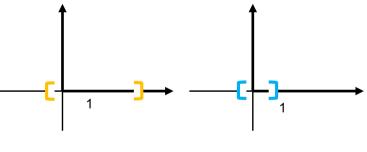
$$x := x - mean(x)$$

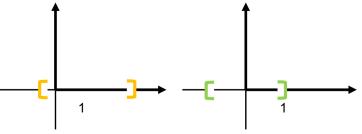


Range of 1



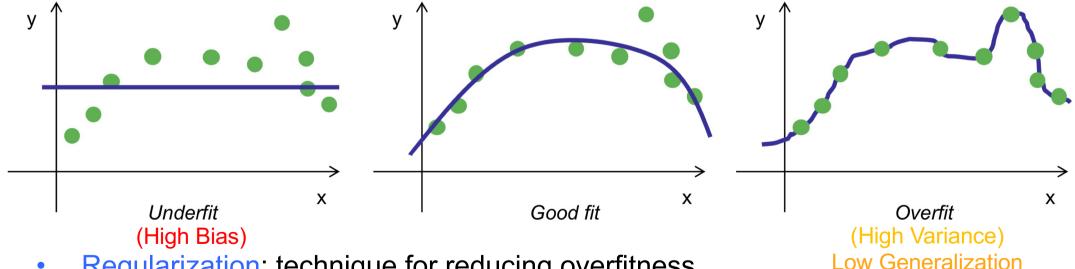






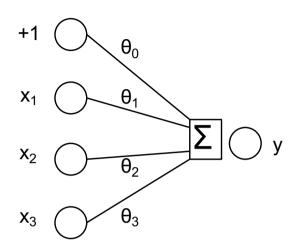
## **Best Hypothesis**

- Objective: Find out "best" hypothesis (values of  $\theta_0$  and  $\theta_1$ )
- Best hypothesis means best fit to data
- And not just best fit only to Train data
- Otherwise the best strategy would be to exactly memorize every entry
- Best hypothesis means best fit for future/yet unknown data: Test data
- i.e., with good capacity for Generalization



- Regularization: technique for reducing overfitness
  - Weights decay, to penalize over-preponderant weights
  - Also: Dropout, Early stopping, Dataset augmentation Deep Learning – Music Generation – 2019 Jean-Pierre Briot

## Multiple Linear Regression – More than 1 Variable



$$h(x) = \theta_0 + \theta_1 x_1 + \theta_2 x_2 + \theta_3 x_3$$

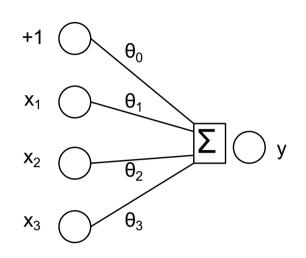
Input Dataset: X:

$$X_1^{(1)}$$
 $X_2^{(1)}$ 
 $X_3^{(1)}$ 

$$X_1^{(2)}$$
 $X_2^{(2)}$ 
 $X_3^{(2)}$ 

Output Dataset: y:

## **Multiple Linear Regression Vectorization**



$$h(x) = \theta_0 + \theta_1 x_1 + \theta_2 x_2 + \theta_3 x_3$$

$$= {}_{i=0}{}^{n} \Sigma \theta_i x_i \quad (with x_0 = 1)$$

$$= [\theta_0 \theta_1 \theta_2 \theta_3] * \begin{bmatrix} 1 \\ x_1 \\ x_2 \\ x_3 \end{bmatrix}$$

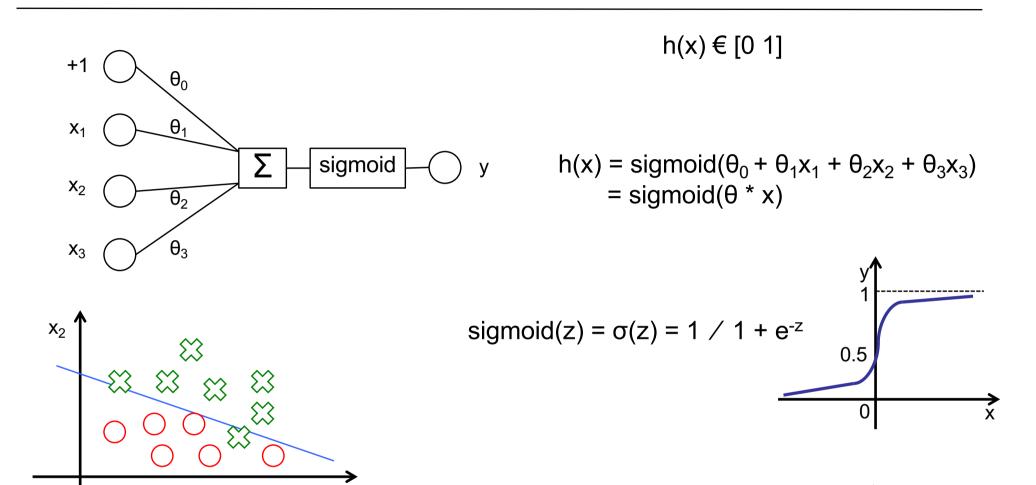
$$scalar(1x1)$$
 =  $vector(1x4)$  \*  $vector(4x1)$   
 =  $\theta$  \*  $x$ 

Computing predictions for a set of examples X:

$$\theta * X = [\theta_0 \; \theta_1 \; \theta_2 \; \theta_3] * \begin{bmatrix} 1 & \dots & 1 \\ x_1^{(1)} & \dots & x_1^{(m)} \\ x_2^{(1)} & \dots & x_2^{(m)} \\ x_3^{(1)} & \dots & x_3^{(m)} \end{bmatrix} = [h^{(1)} \; \dots \; h^{(m)}]$$

$$vector(1x4) * matrix(4xm) = vector(1xm)$$

## Multiple Logistic Regression (Classification)

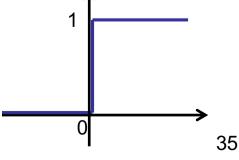


Perceptron [Rosenblatt 1957] used unit step function

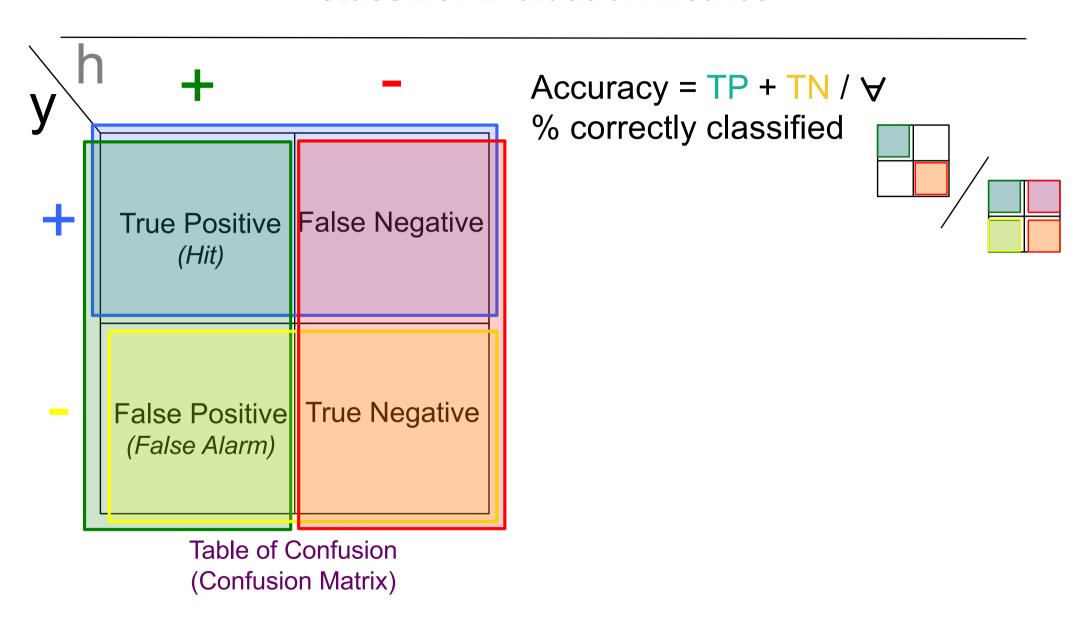
Current Neural Networks use Softmax (transforms into probabilities)

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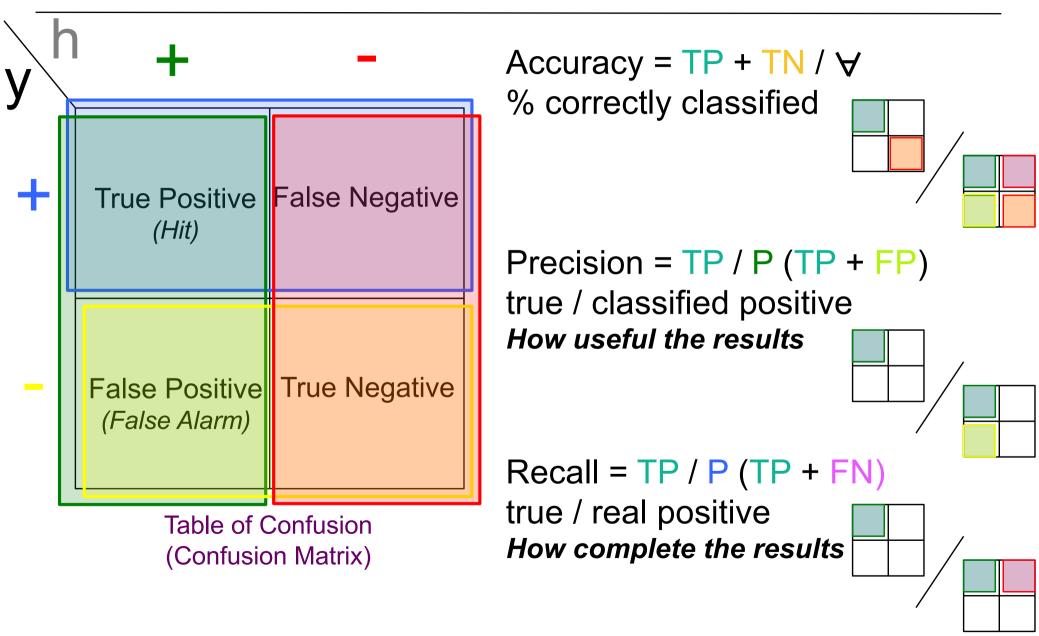
 $X_1$ 

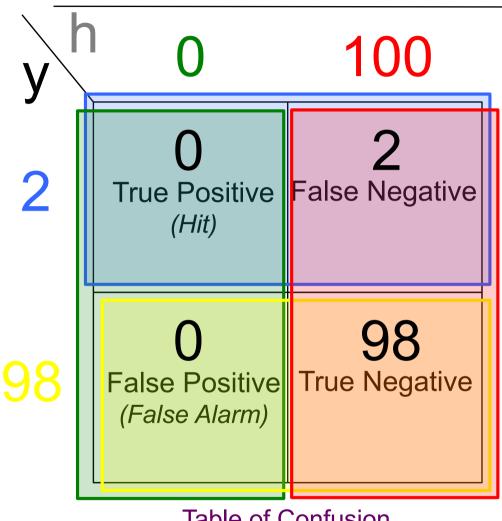


#### **Classifier Evaluation Metrics**



### **Classifier Evaluation Metrics**





Accuracy =  $TP + TN / \forall = 0.98$ 

% correctly classified

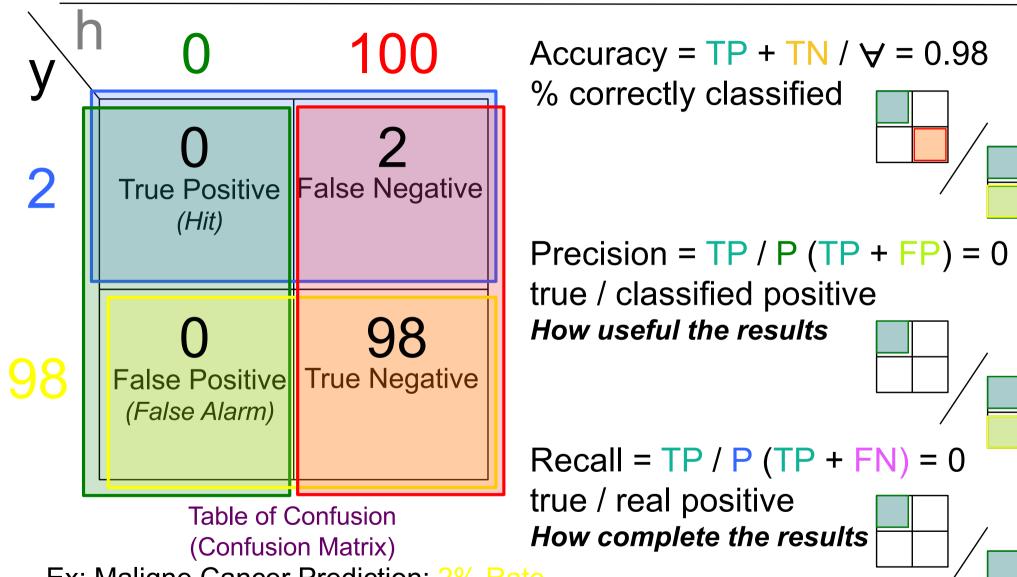
Table of Confusion (Confusion Matrix)

Ex: Maligne Cancer Prediction: 2% Rate

Optimist Hypothese: Always (100%) False

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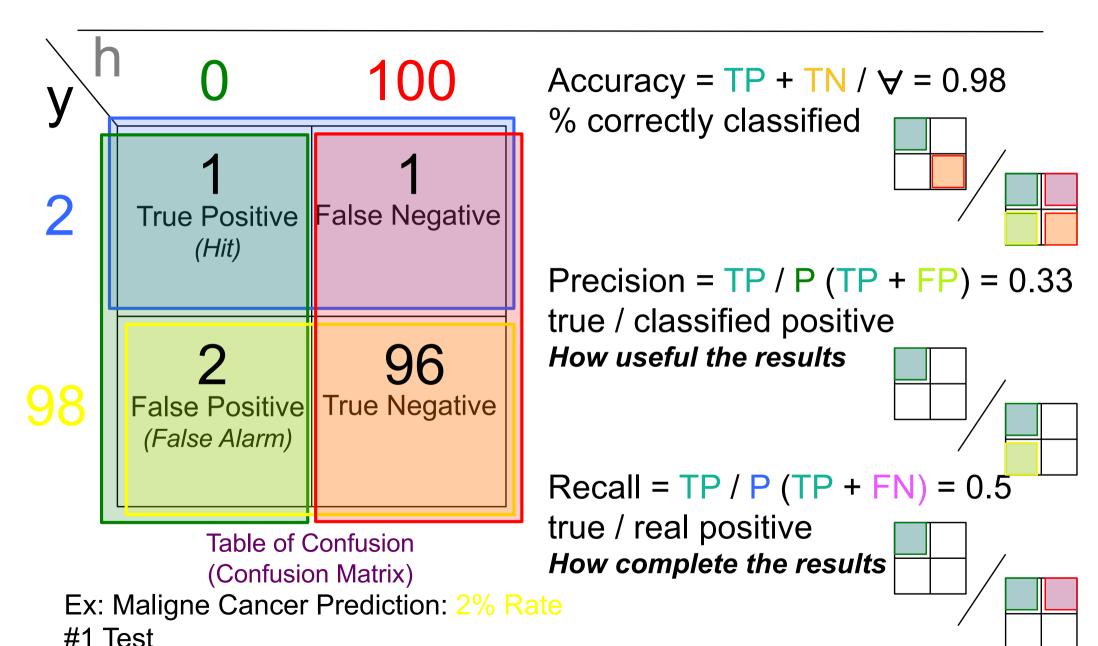


Ex: Maligne Cancer Prediction: 2% Rate

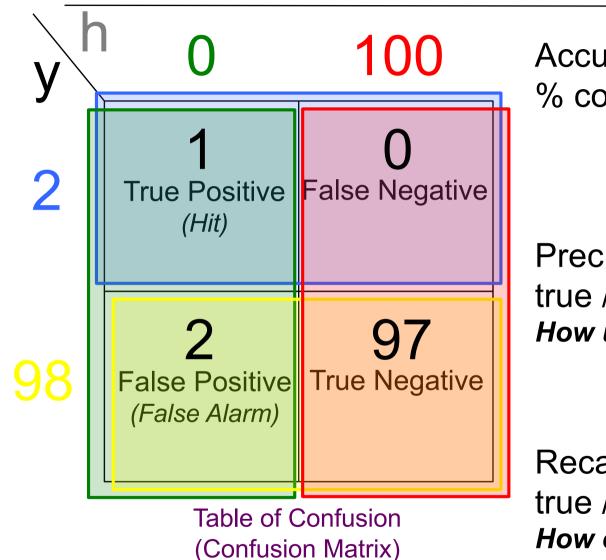
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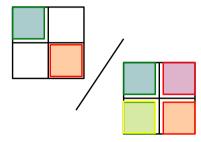


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Accuracy =  $TP + TN / \forall = 0.98$ 

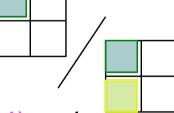
% correctly classified



Precision = TP / P (TP + FP) = 0.33

true / classified positive

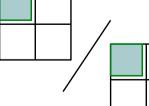
How useful the results



Recall = TP / P (TP + FN) = 1

true / real positive

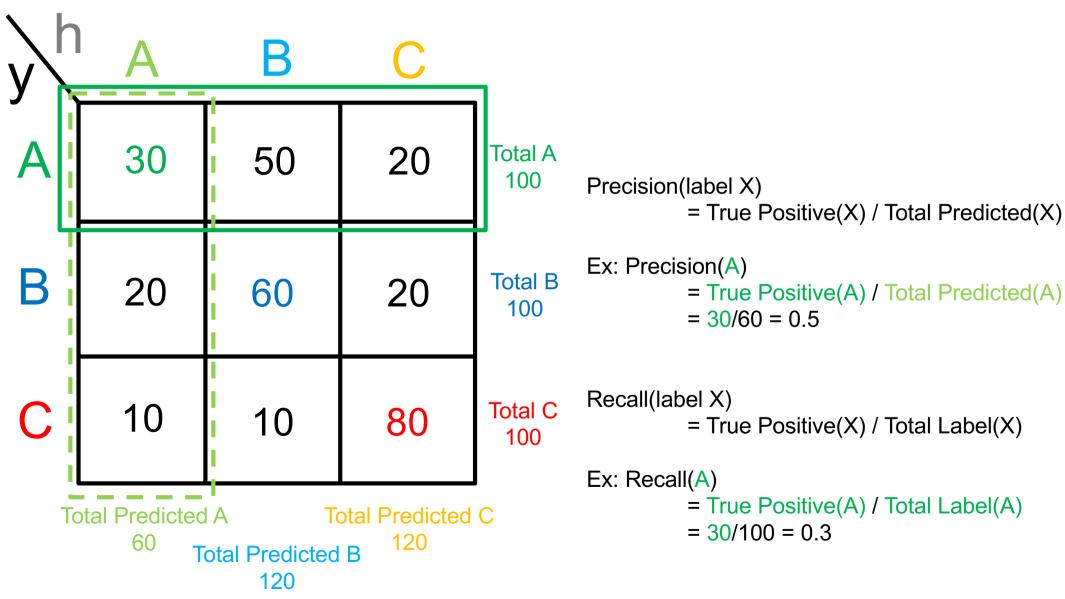
How complete the results



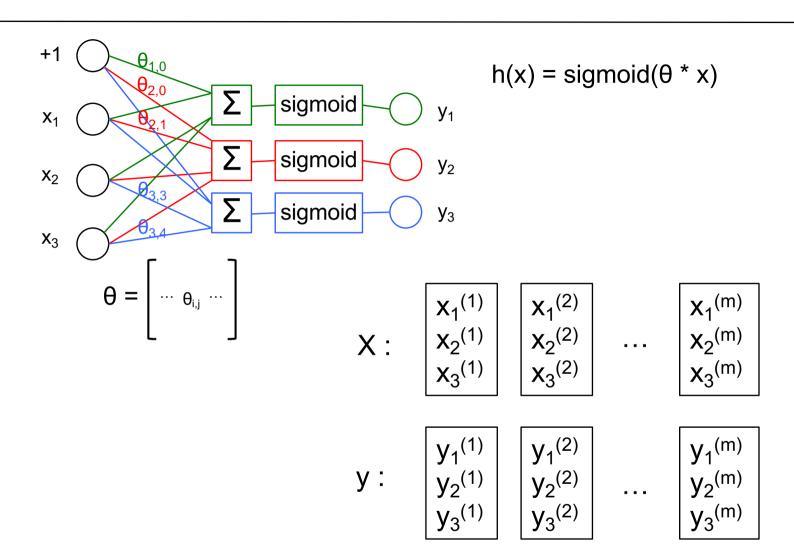
Ex: Maligne Cancer Prediction: 2% Rate

#2 Test

### **Multilabel/class Confusion Matrix**



# Multivariate Multiple Logistic Regression (Classification)



Current Neural Networks use Softmax

### Multivariate Multiple Classification Vectorization

$$h(x) = \begin{bmatrix} h_1(x) \\ h_2(x) \\ h_3(x) \end{bmatrix} = \begin{bmatrix} \theta_{1,0} + \theta_{1,1}x_1 + \theta_{1,2}x_2 + \theta_{1,3}x_3 \\ \theta_{2,0} + \theta_{2,1}x_1 + \theta_{2,2}x_2 + \theta_{2,3}x_3 \\ \theta_{3,0} + \theta_{3,1}x_1 + \theta_{3,2}x_2 + \theta_{3,3}x_3 \end{bmatrix} = \theta * x = \begin{bmatrix} \theta_{1,0} & \theta_{1,1} & \theta_{1,2} & \theta_{1,3} \\ \theta_{2,0} & \theta_{2,1} & \theta_{2,2} & \theta_{2,3} \\ \theta_{3,0} & \theta_{3,1} & \theta_{3,2} & \theta_{3,3} \end{bmatrix} * \begin{bmatrix} 1 \\ x_1 \\ x_2 \\ x_3 \end{bmatrix}$$

$$vector(3x1) = matrix(3x4) * vector(4x1)$$

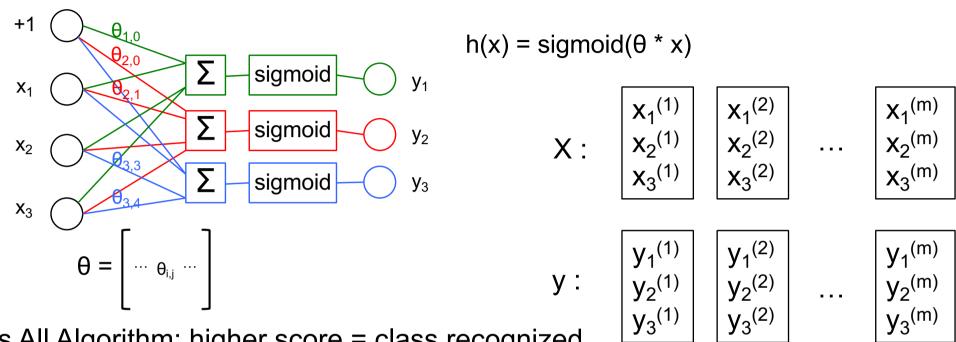
Computing predictions for a set of examples X:

$$\theta * X = \begin{bmatrix} \theta_{1,0} & \theta_{1,1} & \theta_{1,2} & \theta_{1,3} \\ \theta_{2,0} & \theta_{2,1} & \theta_{2,2} & \theta_{2,3} \\ \theta_{3,0} & \theta_{3,1} & \theta_{3,2} & \theta_{3,3} \end{bmatrix} * \begin{bmatrix} 1 & \dots & 1 \\ x_1^{(1)} & \dots & x_1^{(m)} \\ x_2^{(1)} & \dots & x_2^{(m)} \\ x_3^{(1)} & \dots & x_3^{(m)} \end{bmatrix} = \begin{bmatrix} h_1^{(1)} & \dots & h_1^{(m)} \\ h_2^{(1)} & \dots & h_2^{(m)} \\ h_3^{(1)} & \dots & h_3^{(m)} \end{bmatrix} : [class^{(1)} & \dots & class^{(m)}]$$

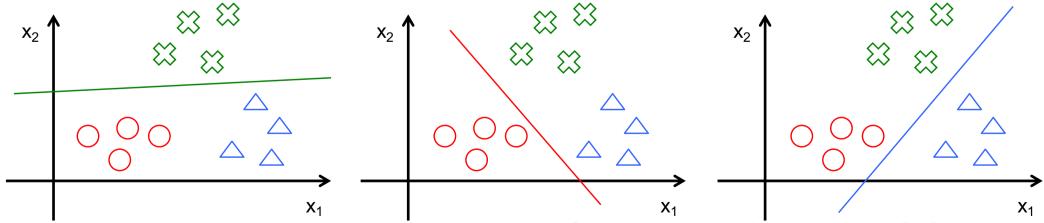
$$matrix(3x4) * matrix(4xm) = matrix(3xm) * vector(1xm)$$

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### Multivariate Multiple Logistic Regression (Classification)



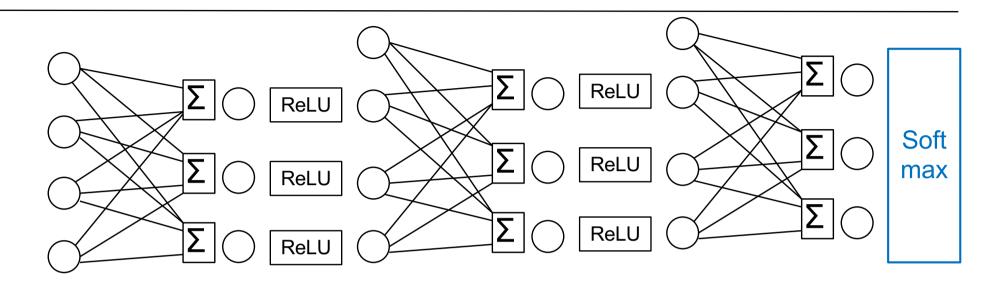
One vs All Algorithm: higher score = class recognized



Current Neural Networks use Softmax

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### **Modern Neural Network**



Softmax transforms values into probabilities

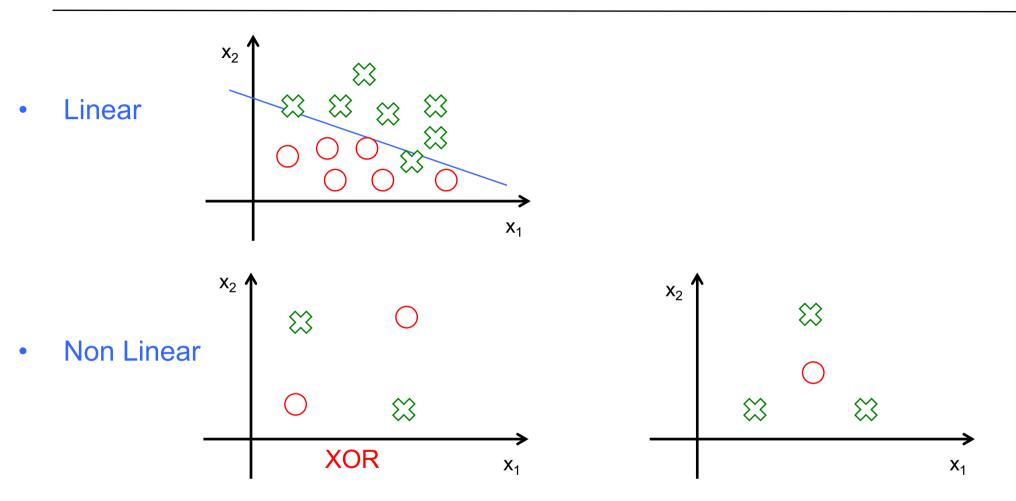
$$\sigma(z)_i = e^{z_i} / \sum e^{z_j}$$

Generalization of sigmoid

Associated cost function is cross entropy

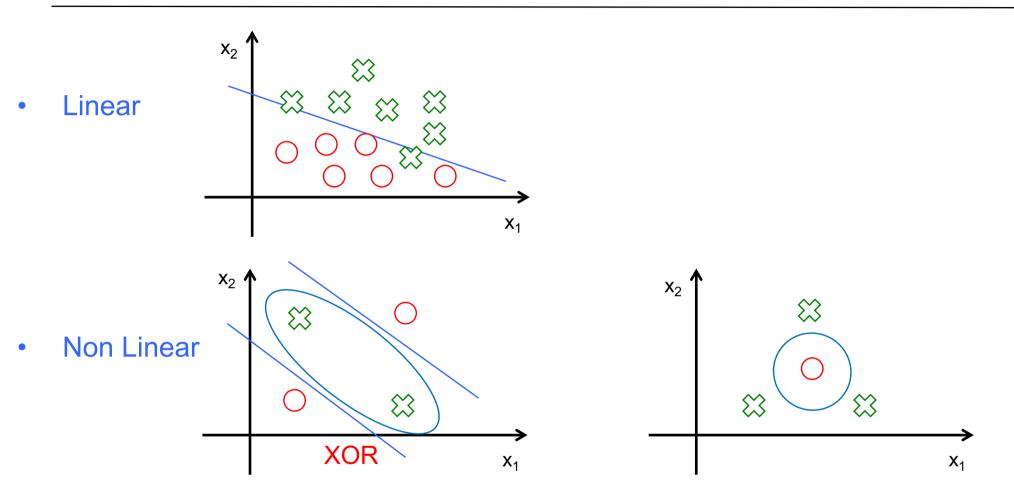
# **Non Linearity**

### **Linear vs Non Linear Decision Boundary**



- Argument (XOR) used by [Minsky & Papert 1969] to criticize Perceptrons [Rosenblatt 1957] (and advocate Symbolic Artificial Intelligence)
- This stopped research on Perceptrons/Neural Networks for a long while
- until Hidden Layers and Backpropagation or/and Kernel Trick (see later)
   Jean-Pierre Briot Deep Learning Music Generation 2019

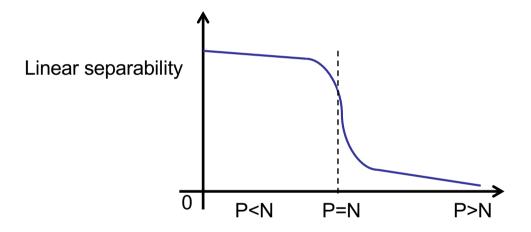
### **Linear vs Non Linear Decision Boundary**



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   Jean-Pierre Briot Deep Learning Music Generation 2019

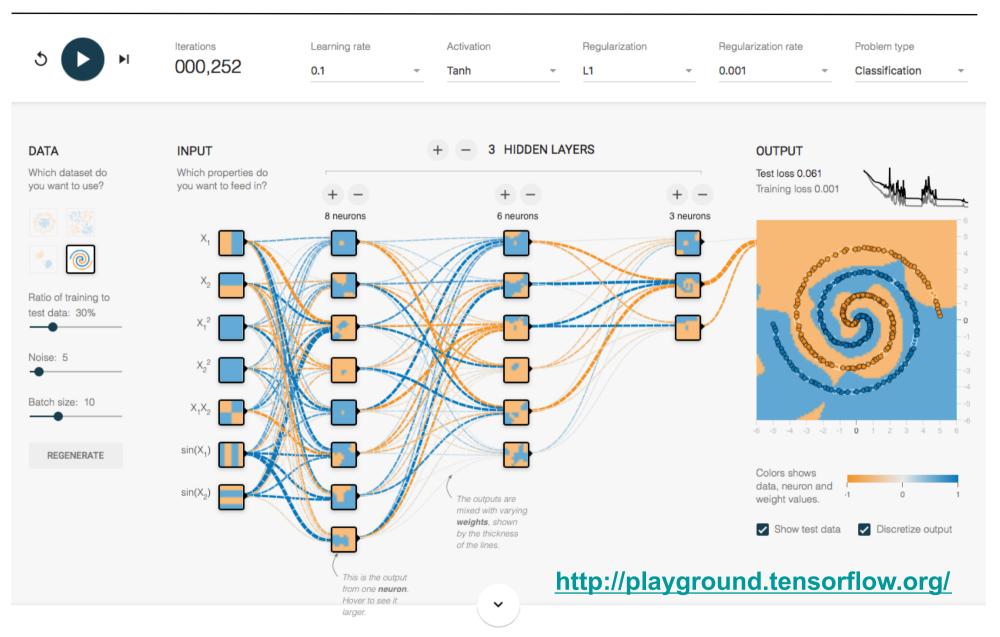
### **Linear vs Non Linear Decision Boundary**

- A consequence of Cover's Theorem [Cover, 1966]
  - The probability that P samples (examples) of dimension N (number of parameters) are linearly separable goes to zero very quickly as P grows larger than N

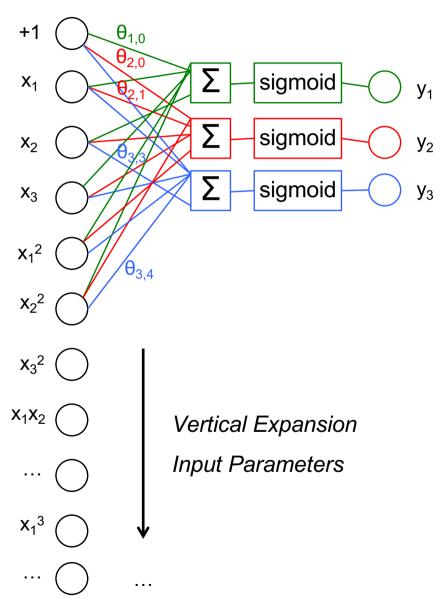


[LeCun 2016]

# **Example (TensorFlow PlayGround)**



# 1<sup>st</sup> Approach: Polynomial Logistic Regression



Jean-Pierre Briot

### 1<sup>st</sup> Approach: Polynomial Logistic Regression

#### Idea:

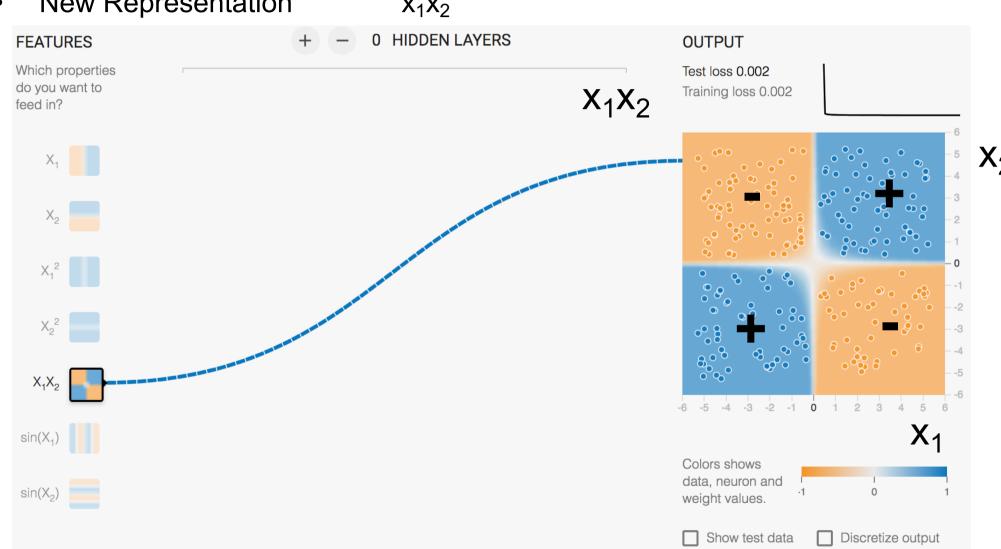
- Increase the number of Dimensions
- By adding Polynomial Inputs
  - » Quadratic: x<sub>1</sub><sup>2</sup>, x<sub>2</sub><sup>2</sup>...
     » Dot products: x<sub>1</sub>x<sub>2</sub>, x<sub>1</sub>x<sub>3</sub>...
     » Cubic: x<sub>1</sub><sup>3</sup>, x<sub>2</sub><sup>3</sup>...
  - » Sinus:  $sin(x_1)$ ,  $sin(x_2)$ ...
  - **»** ...
- In order to find (explore) a higher Dimension Space in which could be found a Linear Decision Boundary

#### Problems:

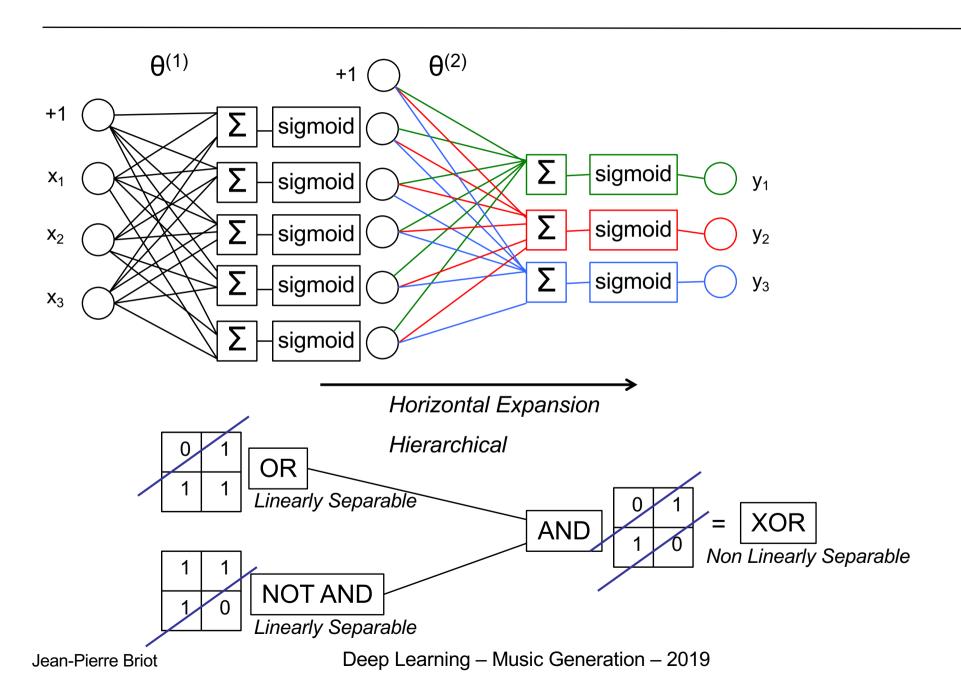
- Select the Additional Inputs
- Add them in a combinatorial way
- The Number of Inputs could become Very Large
- Computation and Data becomes more Heavy

# Example: $x_1x_2$

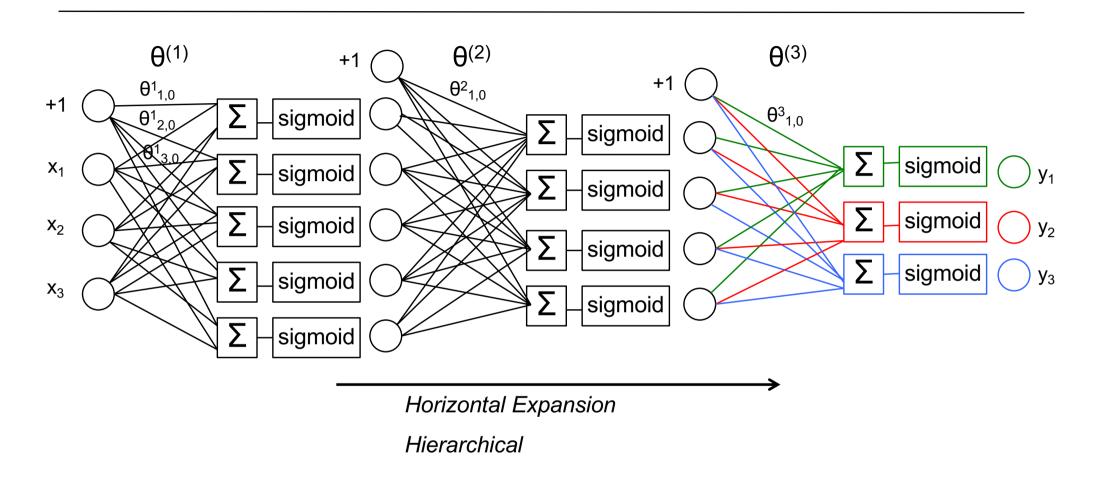
- **Initial Representation**  $X_1 \times X_2$
- **New Representation**  $X_1X_2$



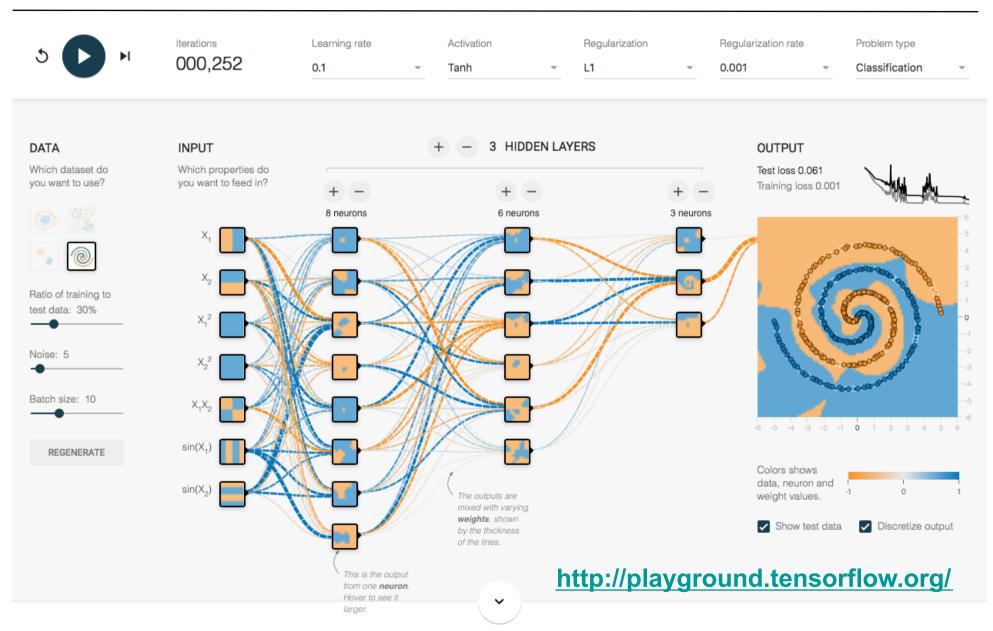
# 2<sup>nd</sup> Approach: Hidden Layers



# 2<sup>nd</sup> Approach: Hidden Layers



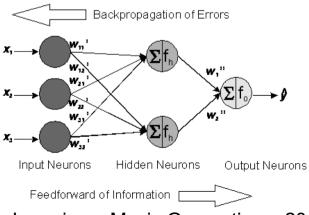
# **Example (TensorFlow PlayGround)**



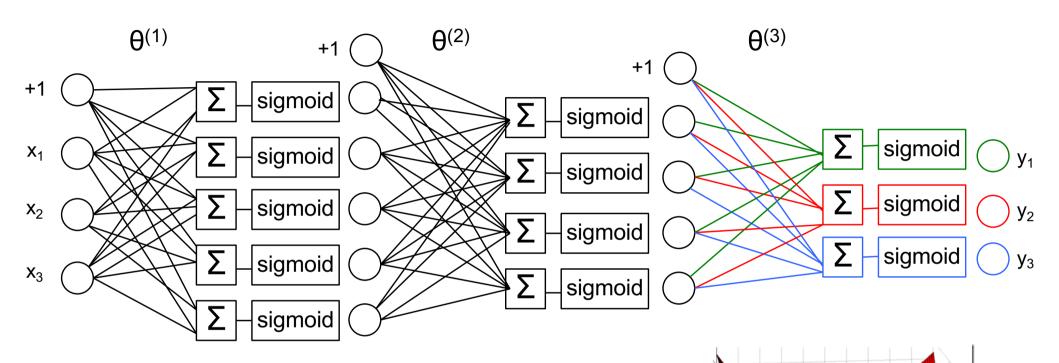
### **Backpropagation**

#### Issue:

- How to compute Gradients (partial derivatives respective to each θ<sup>(k)</sup><sub>i,j</sub> (weight)) ?
- Now that there are several hidden layers...
- Backpropagation (backward propagation of errors) algorithm [Rumelhart et al. 1986, initial ideas since 1960] estimates the gradients for each weight θ<sup>(k)</sup><sub>i,j</sub> (in each layer k), through a chain rule approach:
  - Feedforward the network to compute the output
  - Compute output layer units errors (deltas between predicted and actual values)
  - Propagate backward the errors (deltas) to each unit of previous layer
  - And then compute (accumulate) the gradients (relative to each weight)



# 2<sup>nd</sup> Approach: Hidden Layers – Limits



- Non Convex Optimization
  - Importance/Difficulty of Initialization of Weights  $(\theta^{(n)}_{i,i})$
  - **Local Minimum**



- Backpropagation algorithm (chain rule based) to propagate gradients (from output errors)
- Thinner Estimation (Increasing errors) of gradients while traversing layers

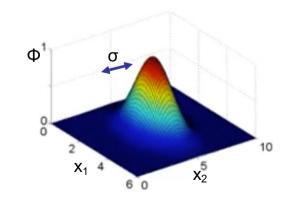
# 3<sup>rd</sup> Approach: Kernel (Trick)

- Increase the number of Dimensions
- By a Transformation of Input Parameters into a Linearly Separable Higher Dimension Feature Space
- A Change of Representation
- This Transformation Function K is Named a Kernel Function
- A Kernel function  $K(x^{(1)}, x^{(2)})$  represents the *Similarity* between two examples  $(x^{(1)} \text{ and } x^{(2)})$
- Example of Kernel: Gaussian Kernel
  - also named Radial Basis Function (RBF) Kernel
  - $K(x^{(j)}, I^{(i)}) = similarity(x^{(j)}, I^{(i)}) = exp(-||x^{(j)} I^{(i)}||^2/2\sigma^2)$



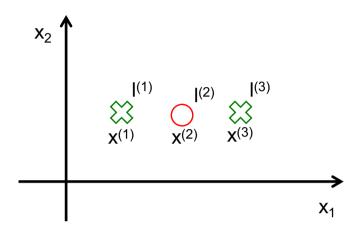
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- » Linear (Without) Kernel, Polynomial Kernel, Sigmoid Kernel...
- » Homemade Kernel (must satisfy Mercer property [Mercer 1909])



# **Kernel = Samples-Centered Feature Transformation**

Let's consider all (m = 3) examples  $x^{(i)}$  as Landmarks  $I^{(i)}$ 

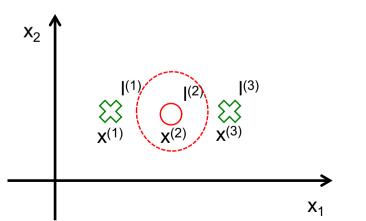


Features are defined as following:

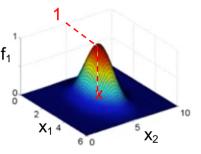
- 
$$f_1(x) = K(x, I^{(1)}) = \exp(-||x - I^{(i)}||^2/2\sigma^2)$$

$$- f_2(x) = K(x, I^{(2)})$$

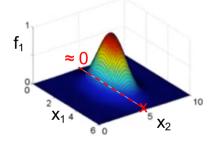
$$- f_m(x) = K(x, I^{(m)})$$



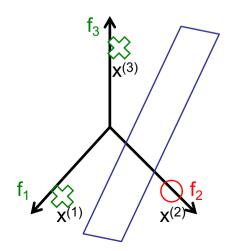
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$$f_1(x^{(1)}) = K(x^{(1)}, I^{(1)}) = 1$$



$$f_1(x^{(1)}) = K(x^{(1)}, I^{(1)}) = 1$$
  $f_1(x^{(2)}) = K(x^{(2)}, I^{(1)}) \approx 0$ 



### **Kernel Trick**

 Computing the Kernel is much easier (and more efficient) when it can be expressed as an inner product (in the feature space) of a kernel function f

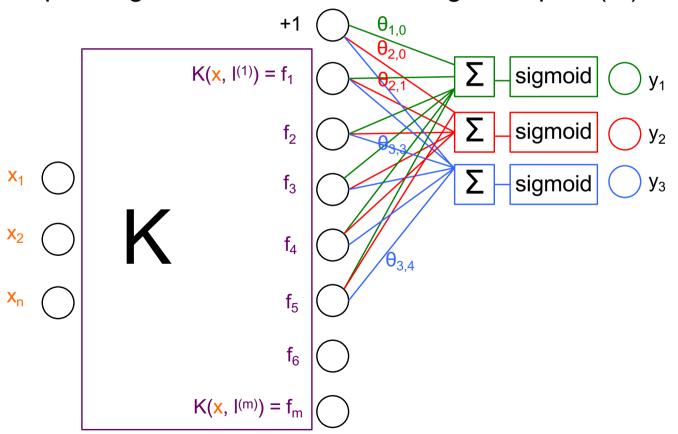
• 
$$K(x^{(1)}, x^{(2)}) = f(x^{(1)}).f(x^{(2)})$$

• Ex: K(x, y) = 
$$(\langle x_1, x_2 \rangle, \langle y_1, y_2 \rangle)^2$$
  
=  $(x_1y_1 + x_2y_2)^2$   
=  $x_1^2y_1^2 + 2x_1y_1x_2y_2 + x_2^2y_2^2$   
=  $\langle x_1^2, \sqrt{2} x_1x_2, x_2^2 \rangle, \langle y_1^2, \sqrt{2} y_1y_2, y_2^2 \rangle$   
= f(x). f(y)  
with f(x) =  $\langle x_1^2, \sqrt{2} x_1x_2, x_2^2 \rangle$ 

Mercer's Theorem: Characterization of a function as a kernel function

# Kernel (Trick)

- The initial n dimension space (number of parameters) is tranformed into a m (number of Training examples) dimension space of features (new parameters), linearly separable
- This new space is independent from the number of parameters (n) and so
  depending on the number of training examples (m)



#### Note:

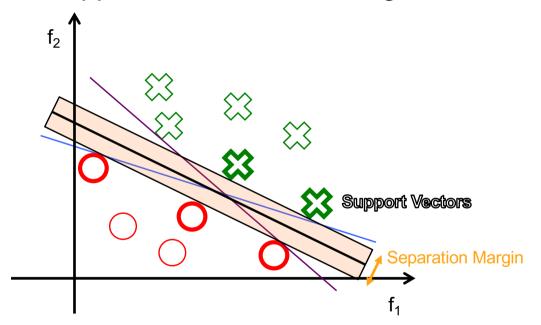
There are 2 phases:

- Configuration of the
   Kernel component with
   Training examples –
   landmarks, I<sup>(1)</sup>,... I<sup>(m)</sup> are
   set and stored into the
   Kernel component
- Application of the Kernel component as a dimension transformation on examples (X -> F)

Kernel

### **Support Vector Machines**

- The same Kernel Trick is used by Support Vector Machines
- Support Vector Machine [Boser et al. 1992] [Vapnik 1995]
  - = Kernel [Mercer 1909] + Linear Support Vector Machine [Vapnik & Lerner 1963]
- A Linear Support Vector Machine is good at maximizing the Separation Margin

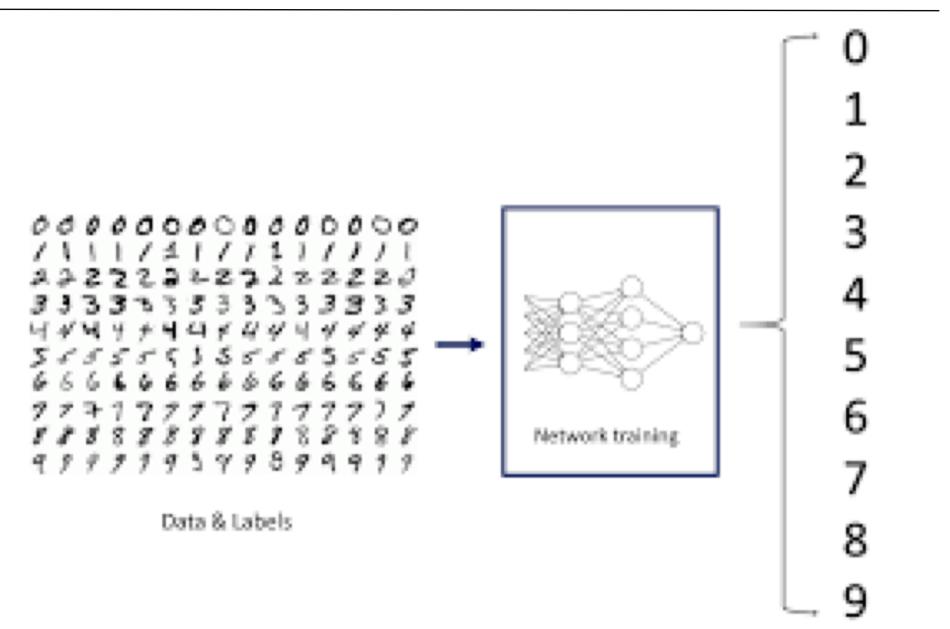


- From 2000's, SVMs outperformed Neural Networks and led to the decrease of research in Neural Networks
- Until the 2010's, when they returned through the idea of Deep Networks/Learning (see later)

### **MNIST Handwritten Character Recognition Test Case**

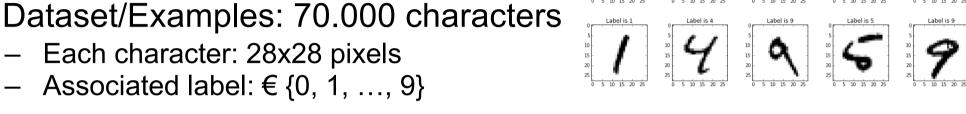


### **MNIST Handwritten Character Recognition Test Case**



### MNIST Handwritten Character Recognition Test Case

- Program in Keras (Python)
- Dataset/Examples: 70.000 characters





- Training Set (60.000)
- Evaluation (Testing) Set (10.000)
- Scaling of data
  - Pixel: Grayscale € (0, 255)
  - Divide by 255
- Input: X = vector of vectors of characters
- Output: y = vector of corresponding labels
  - One-hot encoding of label

label	encoding	labels
3	0 0 0 1 0 0 0 0	0 1 2 3 4 5 6 7 8

# MNIST Handwritten Character Recognition Test Case Programs

### Standard

- 2 Hidden Layers (512 units)
- Regularization (Dropout)
- 10 Epochs
- Accuracy: 98.33 %

### Simplified

- 1 Hidden Layer (100 units)
- No Regularization
- 5 Epochs
- Accuracy: 92.25 %

### Convolutional

- 4 Hidden Layers
  - » 2 Convolutional (30 and 15 units) and 1 Pooling
  - » Dense (128, 50)
- Regularization (Dropout)
- 10 Epochs
- Accuracy: 99.11 %

### **Determinism vs Stochastic (Sampling)**

- Neural Networks are Deterministic
- As opposed to ex. Markov Chains, MDPs and RBMs, where Production (Sampling) is Stochastic, with Distribution Properties Expected

### Learning

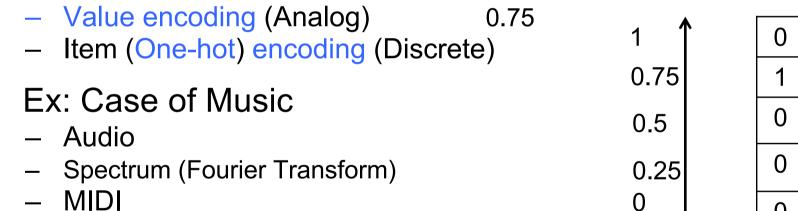
#### **Production**

Deterministic	Gradient Descent	Neural Networks
Stochastic	Stochastic Gradient Descent (SGD)	<ul> <li>Neural Networks with Sampling</li> <li>Markov Chains</li> <li>Markov Decision Processes (MDP) and Reinforcement Learning</li> <li>Restricted Boltzmann Machines</li> </ul>

(RBM)

### Representation (Embeddings)

- Importance of the choice of Representation
- Direct
- **Features** 
  - Manual
  - Extracted by autoencoders
- Encoding



- Piano Roll
- Text
- Time
- Quantization
- Fermata, Tonality...

0

### **Universal Approximator**

- The combination of hidden layer and non linear activation function makes the neural network an universal approximator, able to overcome the non linear separability limitation
- The universal approximation theorem [Hornik, 1991] states that a feedforward network with a single hidden layer containing a finite number of neurons can approximate a wide variety of interesting functions when given appropriate parameters (weights)
- Meanwhile, there is no guarantee that the neural network will learn it!

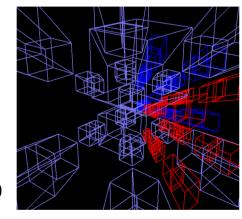
### No Free Lunch!

- The no free lunch theorem for machine learning [Wolpert, 1996] states that, averaged over all possible data-generating distributions, every classification algorithm has the same error rate when classifying previously unobserved points.
- No machine learning is universally any better than any other.
- The most sophisticated algorithm we can conceive has the same average performance, over all possible tasks, as merely predicting that every point belongs to the same class [Goodfellow *et al.*, 2016].
- But, these results hold when we average over all possible data-generating distributions.
- Real applications/data are specific, as well as related algorithms, and have some regularities and inner structure that an algorithm can exploit.

### The Malediction of High Dimensionality [Mallat, 2018]



- Ex: Image with 2,000 x 1,000 pixels with color
- $\bullet$  = 6.000.000 bits
- Space of dimension 6.000.000 !!

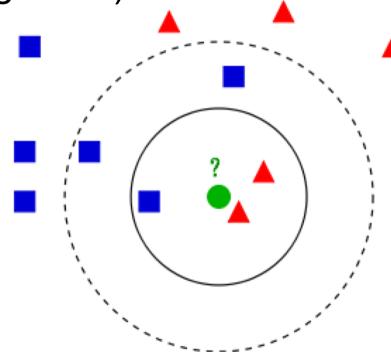


#### The Malediction of High Dimensionality [Mallat, 2018]

Ex. of Task: Image recognition (Classification Task)

kNN algorithm (k Nearest Neighbors)

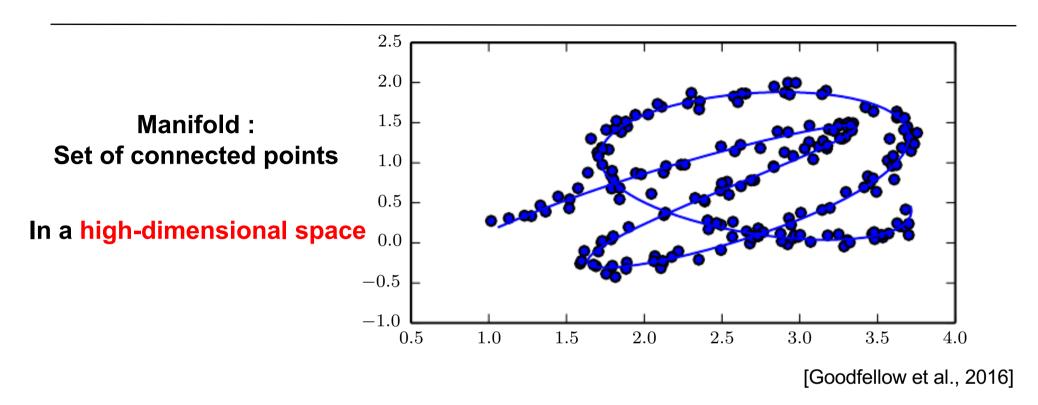
 The class of an element = majority class of k nearest neighbors



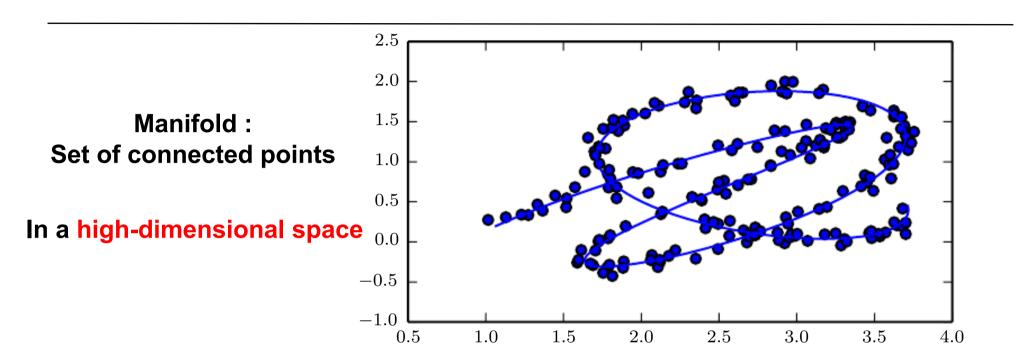
#### Problem:

 Euclidean distance is unhelpful in high dimensions because all vectors are almost equidistant to the query vector

#### Representation/Manifold Learning

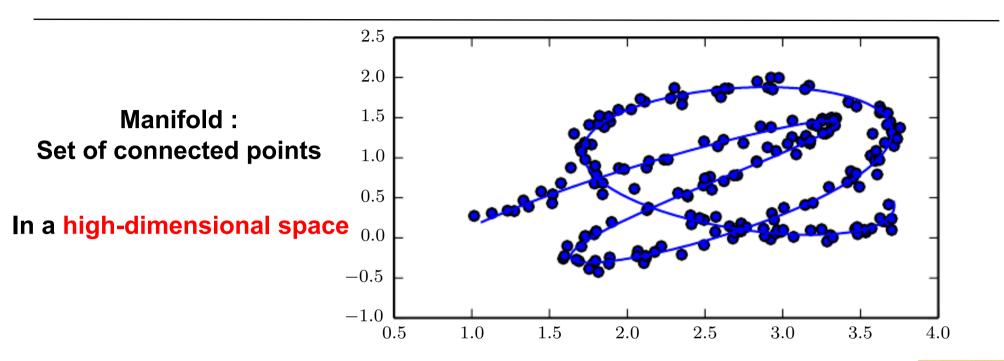


#### Representation/Manifold Learning

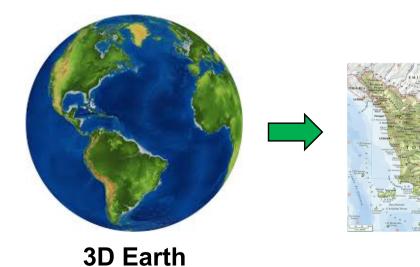


But can be approximated by a smaller number of dimensions, each dimension corresponding to a local variation

#### Representation/Manifold Learning



But can be approximated by a smaller number of dimensions, each dimension corresponding to a local variation



Toscana

Toscana

Toscana

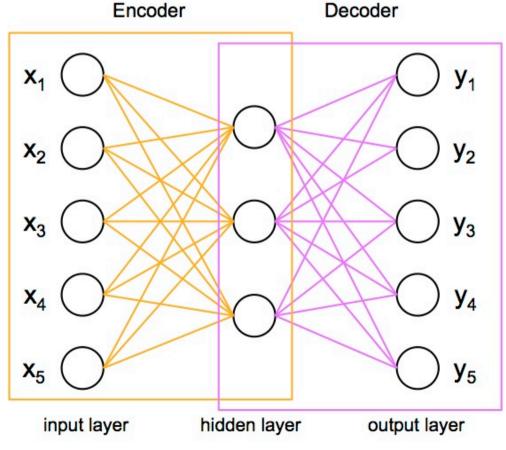
Toscana

**Analogy:** 

2D Map

#### **Autoencoder**

- Symmetric Neural Network
- Trained with examples as input and output
- Hidden Layer will Learn a Compressed Representation at the Hidden Layer (Latent Variables)

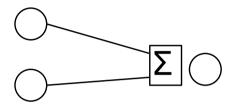


#### **Autoencoder**

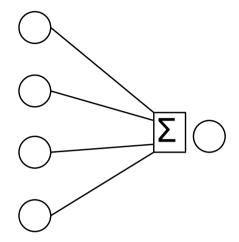
- Autoencoder can do such representation transformation
- Sparse autoencoder
  - Constraint: Sparse activation
  - -> Specialization of each unit/latent variable
  - Feature extractor
- Variational Autoencoder (VAE)
  - Constraint: latent variables follow a Gaussian distribution
  - -> Smooth latent space mapping
  - Representation learning

### Deep Learning Bio-inspired or/and Regression-based?

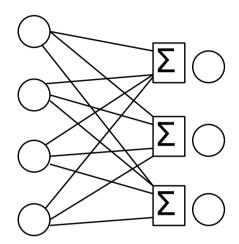
## **Simple Linear Regresssion**



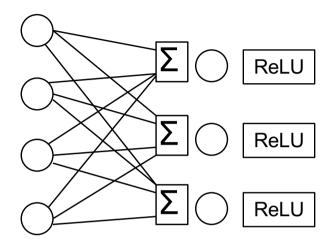
# **Multiple Linear Regression**

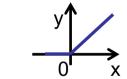


## **Multivariate Multiple Linear Regression**



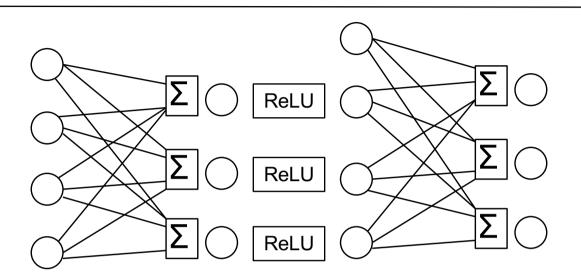
### Non Linear Multivariate Multiple Linear Regression



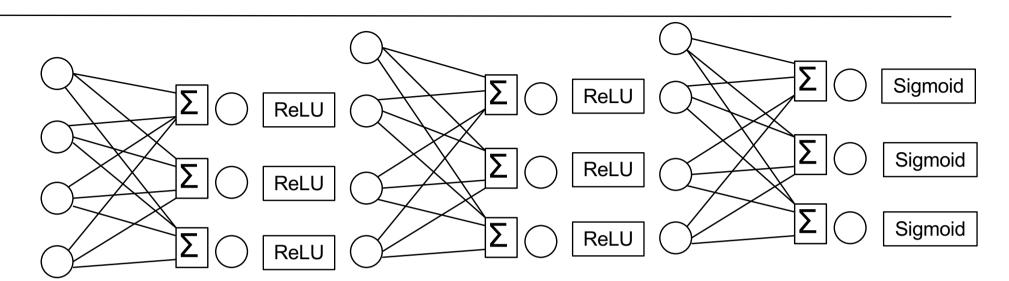


ReLU = max(x, 0) Rectified Linear Unit

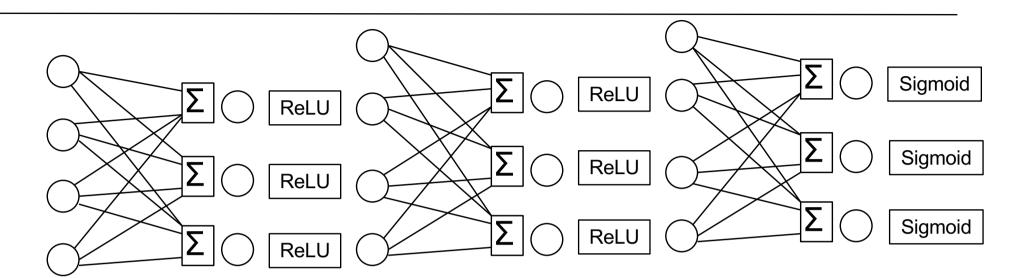
### Multilayer Non Linear Multivariate Multiple Linear Regression



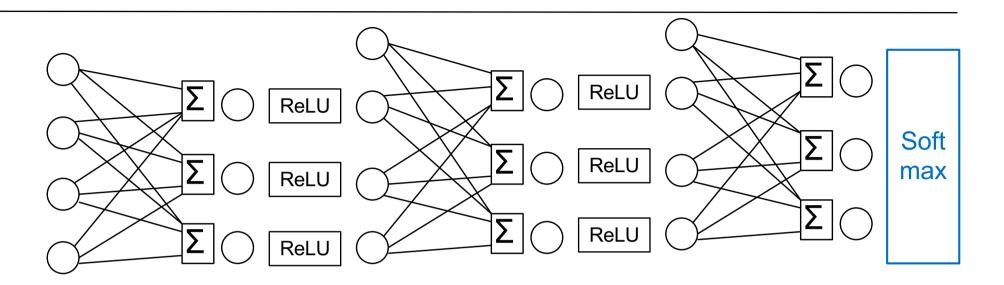
## Multilayer Non Linear Multivariate Multiple Linear Regression



#### = Neural Network



#### **Modern Neural Network**



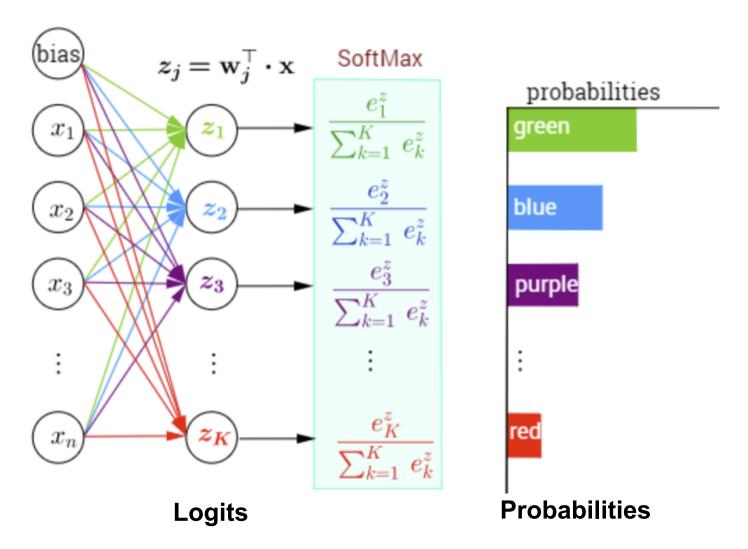
Softmax transforms values into probabilities

$$\sigma(z)_i = e^{z_i} / \sum e^{z_j}$$

Generalization of sigmoid

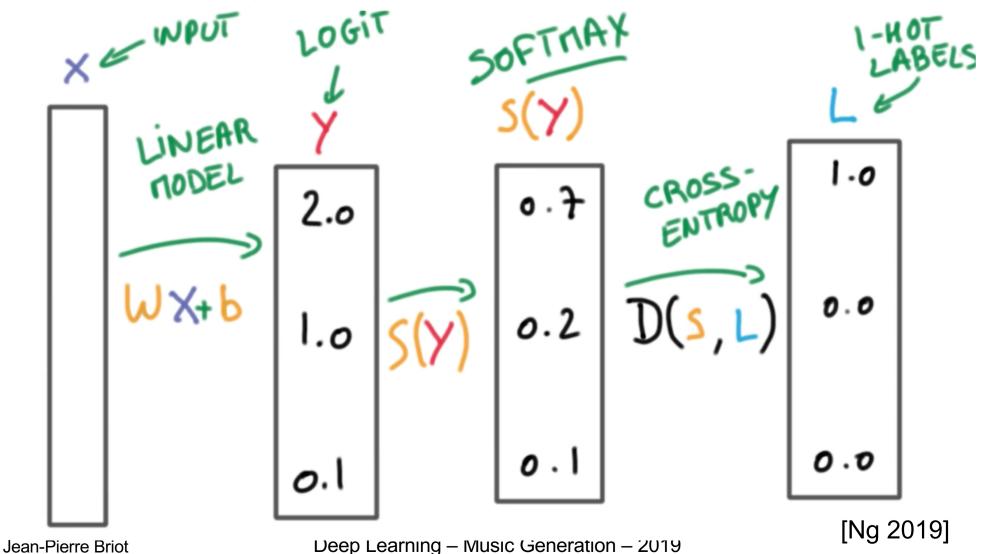
Associated cost function is cross entropy

#### **Softmax**



#### **Softmax + Cross-Entropy**

 Cross-Entropy measures dissimilarity between two probability distributions (prediction and target/true value)

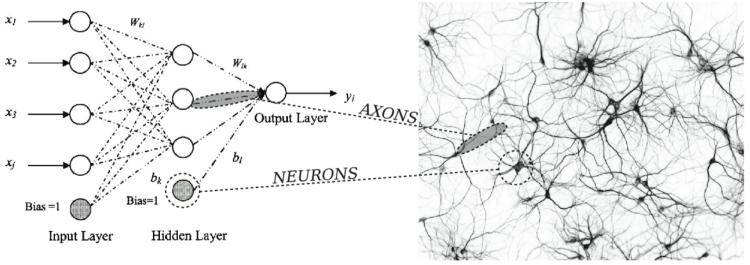


#### Deep Learning Bio-inspired or/and Regression-based?

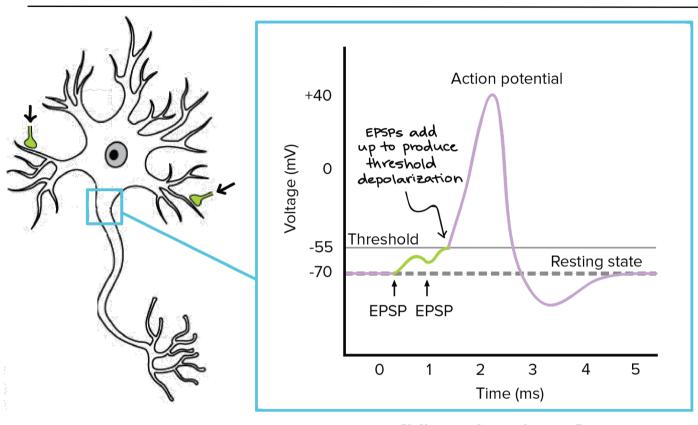
Historically Perceptron bioinspired



#### **NEURAL NETWORK MAPPING**

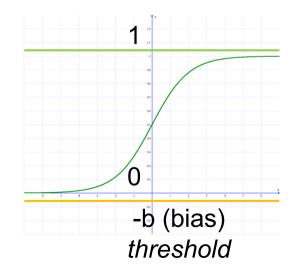


### Deep Learning Bio-inspired or/and Regression-based?



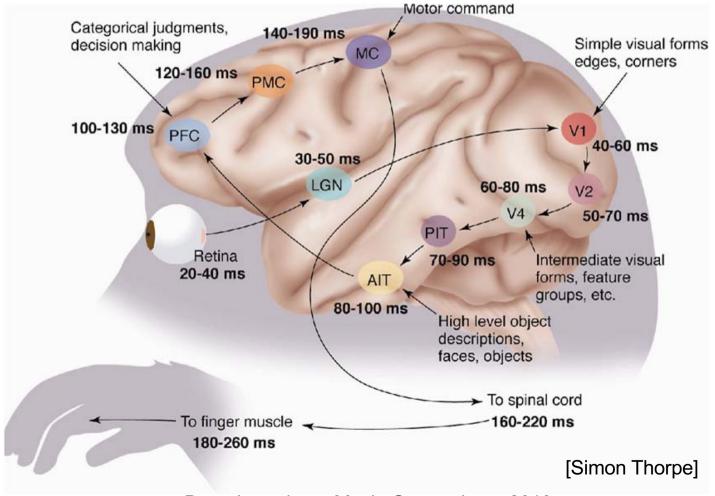
[Khan Academy]

 $sigmoid(\Sigma + b)$ 

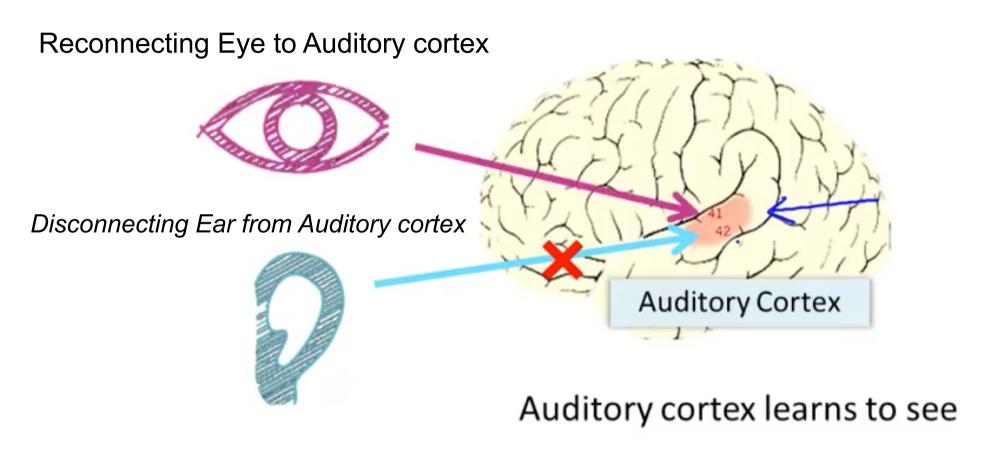


#### **Analogy with Mammalian Visual Cortex**

- Hierarchical
- Multiple Successive Stages
- Intermediate Representations (Features)



### "Universal Learning" Biological Neural Network Hypothesis



[Ng 2011]

#### Deep Learning Bio-inspired or/and Regression-based?

- Convolutional Neural Networks (ConvNets [LeCun et al. 1989]) are bio-inspired
  - Inspired by animal visual cortex [Fukushima1980]
  - Complex neuron cells respond to stimuli in receptive fields (restricted region)

Receptive fields partially overlap

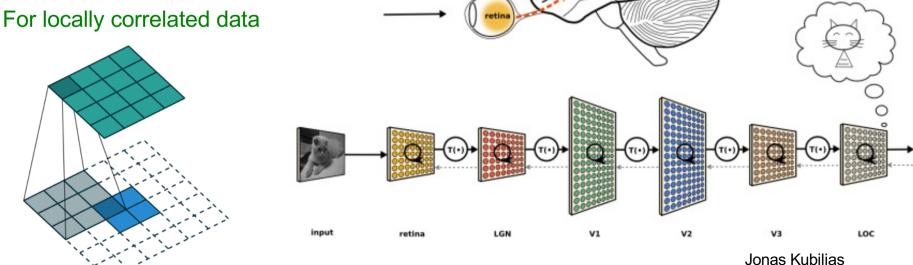
Allows tolerance to input image translation

Weight sharing

Translation invariance

Subsumes (and thus avoids) segmentation

**>>** 



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#### Convolution

#### Convolution

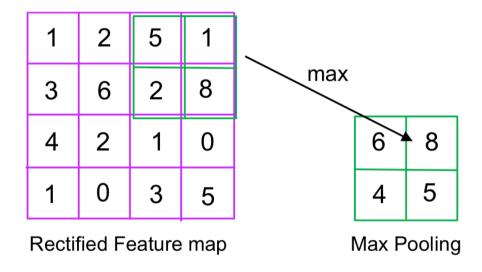
- Slide a matrix (named filter, kernel, or feature detector) through the entire image
- For each mapping position:
  - compute the dot product of the filter with each mapped portion of the image
  - then add all elements of the resulting matrix
- Resulting in a new matrix (named convolved feature, or feature map)

0	1	1	1				
1	0	1	0		1	0	1
0	1	0	0		0	1	0
1	1	1	1		1	0	1
<del>_</del>		Image Filter					

- The size of the feature map is controlled by three hyperparameters:
  - Depth: the number of filters used
  - Stride: the number of pixels by which we slide the filter matrix over the input matrix
  - Zero-padding: if the input matrix is padded with zeros around its border

### **Pooling**

- Reduce the dimensionality of each feature map, while retaining significant information
- Standard operations:
  - max
  - average
  - sum



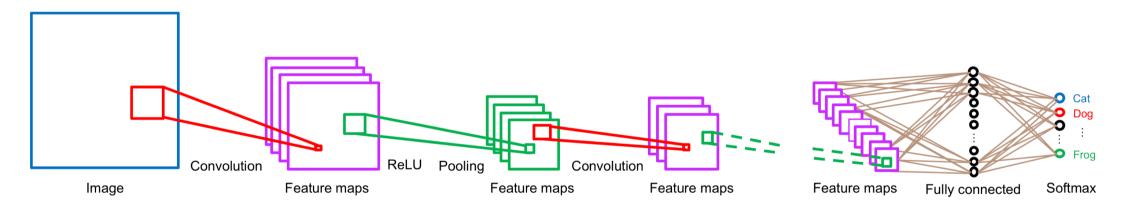
- Parameter sharing used by convolution (shared fixed filter) brings equivariance to translation: a motif in an image can be detected independently of its location
- Pooling brings invariance to small transformations, distortions and translations in the input image





#### Convolution

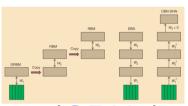
- Full Convolutional architecture:
  - Successive Layers, each Layer with 3 Stages:
    - » Convolution stage
    - » Non linear rectification (ReLU) stage
    - » Pooling stage



## **Techniques**

#### **Techniques**

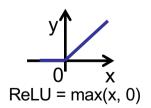
Pre-Training



Efficient Hardware (GPUs)



- Trading Space for Time (and Breadth for Depth) [Bengio & LeCun 2007]
  - More Layers, Cascade/Sequence
- Additional Techniques and Heuristics:
  - Convolution Neural Networks, Clustering, Pooling
  - Recurrent Networks... (See next slides)
  - Memory (LSTM, etc. See next slides)
  - Dropout (as a Regularization technique)
  - ReLU rather than Sigmoid in Hidden Layers
  - SoftMax final Layer



- Restricted Boltzman Machines
  - » Contrastive Divergence Gradient estimation algorithm

#### **Other Variations/Techniques**

Convolutional Neural Networks [LeCun 2010]

- Weight sharing
- Translation invariance
- Subsumes (and thus avoids) segmentation Input
- For locally correlated data
- Pooling (Compress/Factorize)
- Clustering (Group)

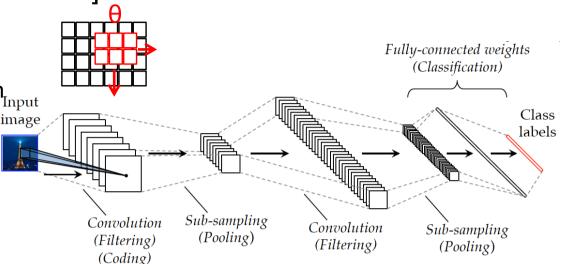
  3 3 3

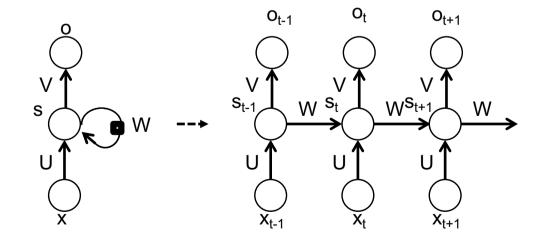
  8 8 8

  8 8 8



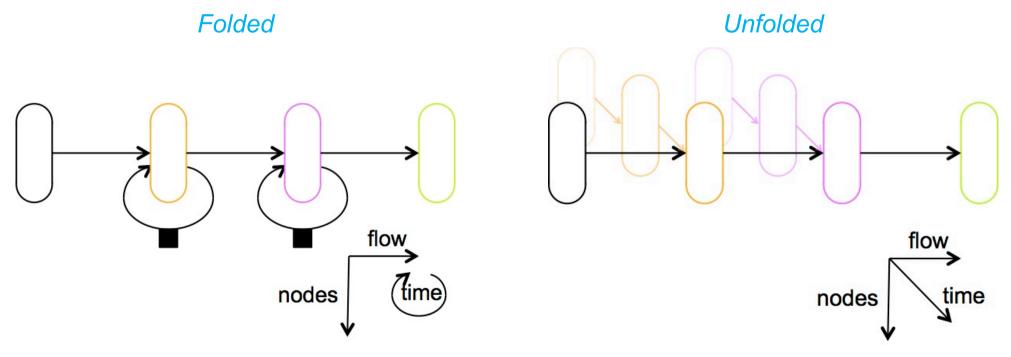
- loop+delay/memory
- for temporal or sequences of data
- ex: Natural Language Processing
- Memory-Augmented Networks
  - LSTM, GRU, Neural Turing Machines
  - Memory access is differentiable thus trainable
  - Attention mechanism





#### **Recurrent Neural Networks (RNN)**

- Recurrent connexion from a layer to itself
- Therefore, the layer learns also from its previous state
- It acts as a memory
- The RNN can learn sequences

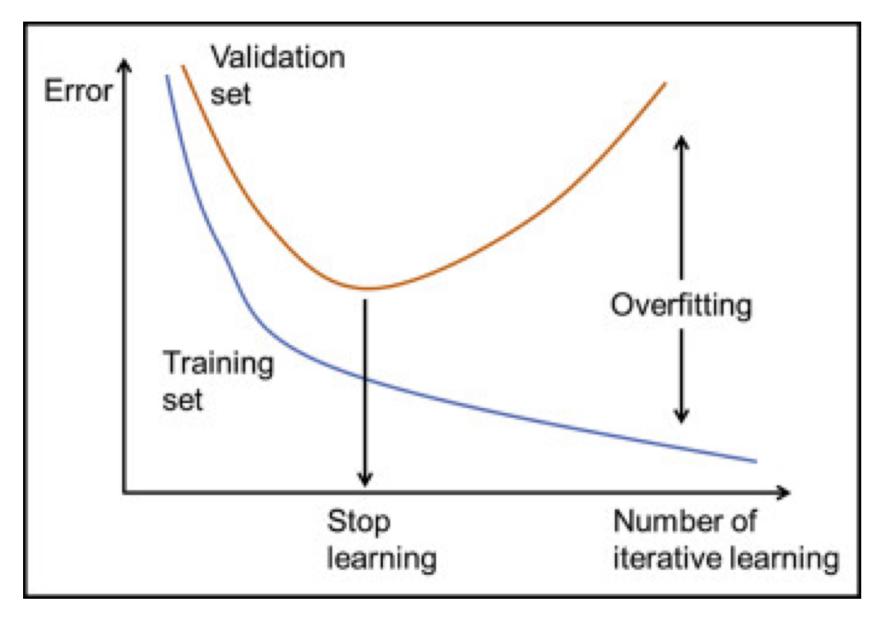


# **Engineering**

#### **Hyperparameters**

- Fine Tuning of Hyperparameters of the Architecture/Model
- Architecture Structure
  - Number of layers
  - Number of units
  - Non linear Function
- Learning Heuristics
  - Cost (Prediction Error): Quadratic, Log, Cross Entropy...
  - Optimization: Gradient Descent, Stochastic, Mini-Batch, Adagrad, Adadelta...
  - Leaning rate
  - Regularization: L1, L2, Dropout...
- Convolution
  - Depth, Stride, Zero-padding
- LSTM
  - Input gate, Output gate, Forget gate biases
- Autoencoder
  - Sparsity
- Seach (Random, Grid, Model-based) for exploring good settings
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#### **Learning Curves**



#### (Deep) Networks Platforms/Libraries

#### 2 Levels:

- Modules: C, Matlab, Packages (Linear algebra...)
- Glue/Scripting/ADL: Architectural description for assembling modules (data flow graph) and system/application management

#### Examples:



- SN, Lush [LeCun & Bottou 1987]
  - Lisp-like (single language)



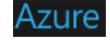
- Torch (Facebook, Google...)
- LuaJIT, Python (PyTorch)



- TensorFlow (Google)
  - Python
- theano Theano (U. Montréal)
  - Python



- Keras
  - Superlayer of (both) TensorFlow and Theano
  - Python

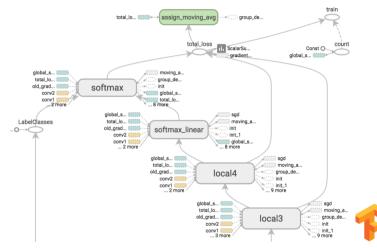


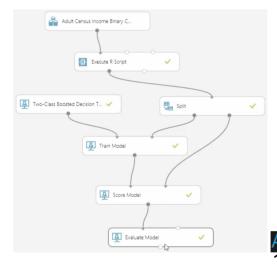
- Azure (Microsoft)
  - Cloud

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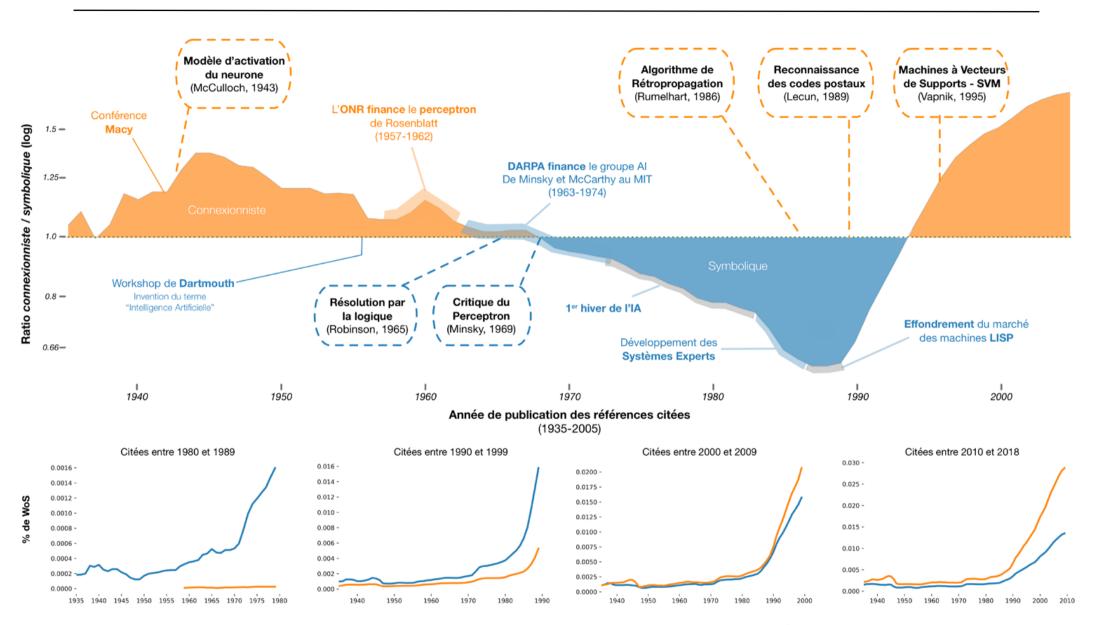
— Drag and Drop



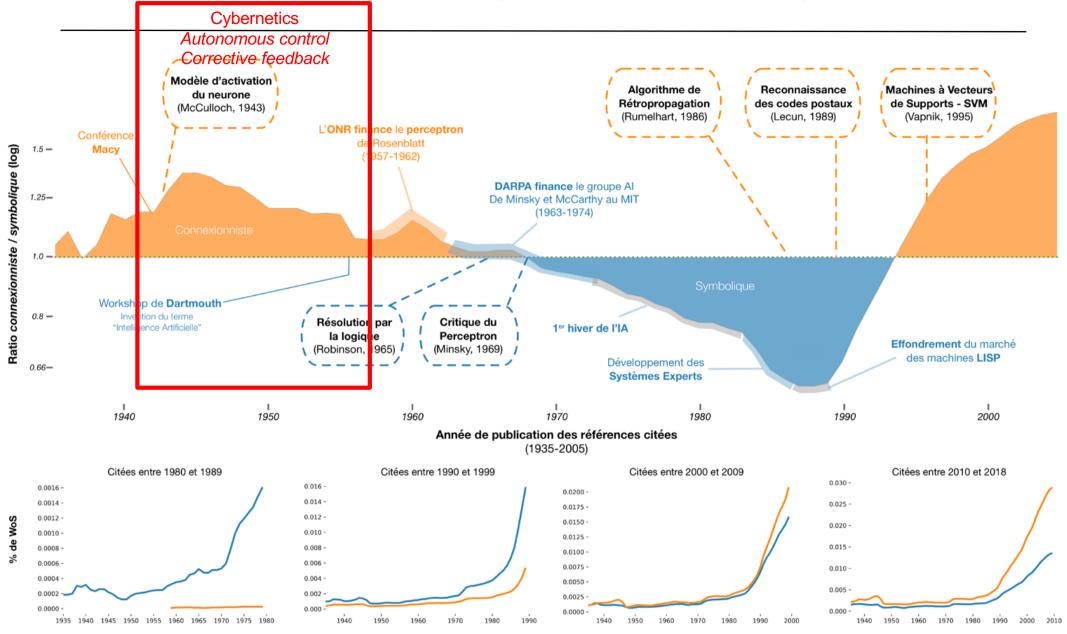


## **History / Various Facets of Al**

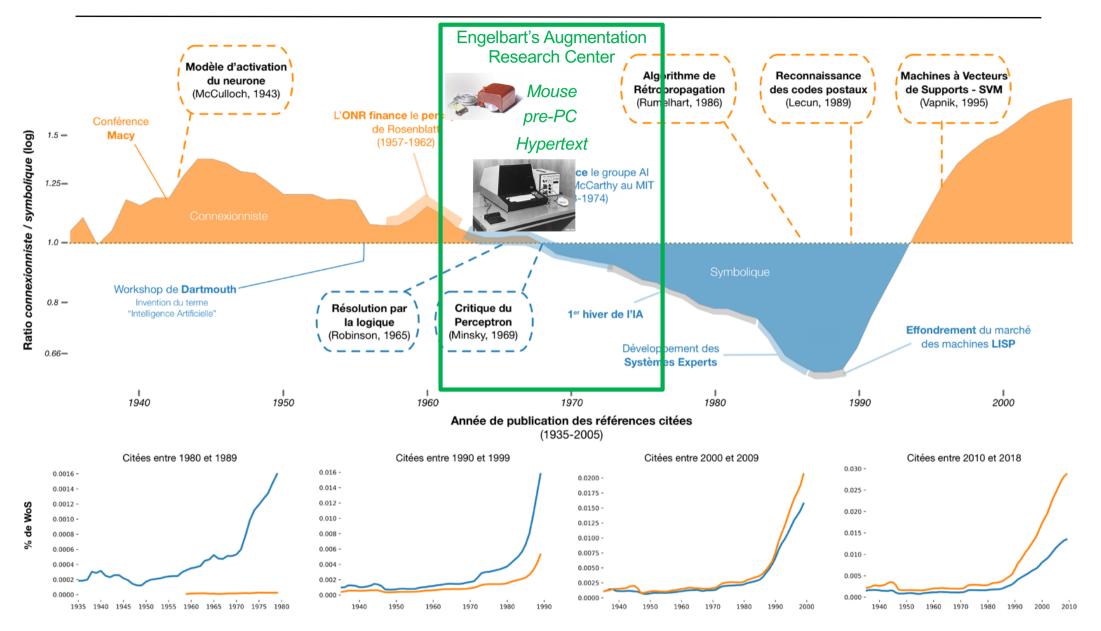
#### Symbolic vs Connexionist AI – History



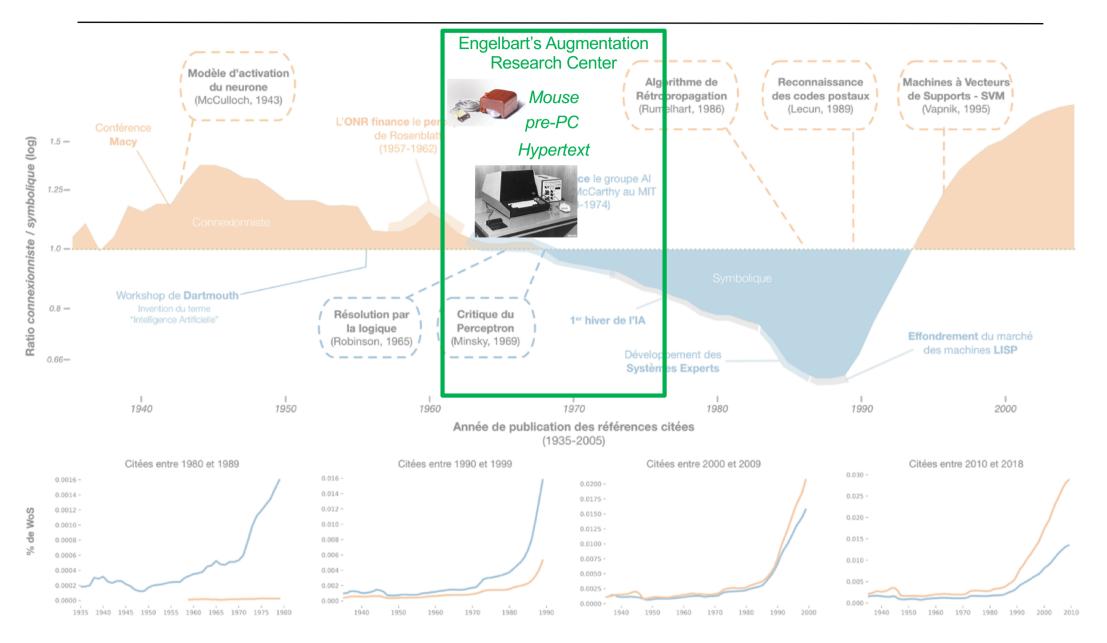
### Symbolic vs Cybernetics – History



#### Al vs IA – History



# Al (Artificial Intelligence) vs IA (Intelligence Augmentation) – History



### **Engelbart's Augmentation Research Center**

- Augmentation Research Center at Stanford Research Institute (SRI)
- Headed by Douglas Engelbart
- Vision of the Interactive Personal Computer
- Mouse
- Graphical Interfaces
- Hypertext
- Visioconference
- Internet









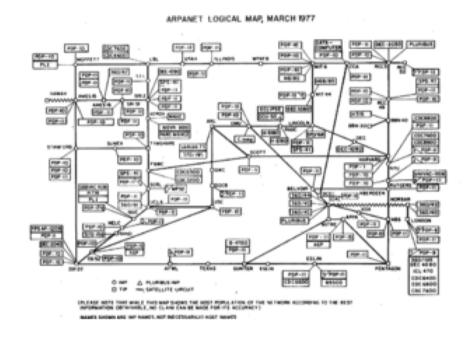
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### **Engelbart's Augmentation Research Center**



Mouse [Engelbart, 1967]



Arpanet [Kleinrock & Engelbart, 1969]

#### Douglas Engelbart Team Demonstration (9 December 1969)



#### monday afternoon

december 9

3:45 p.m. / arena

Chairman:

DR. D. C. ENGELBART Stanford Research Institute Menlo Park, California

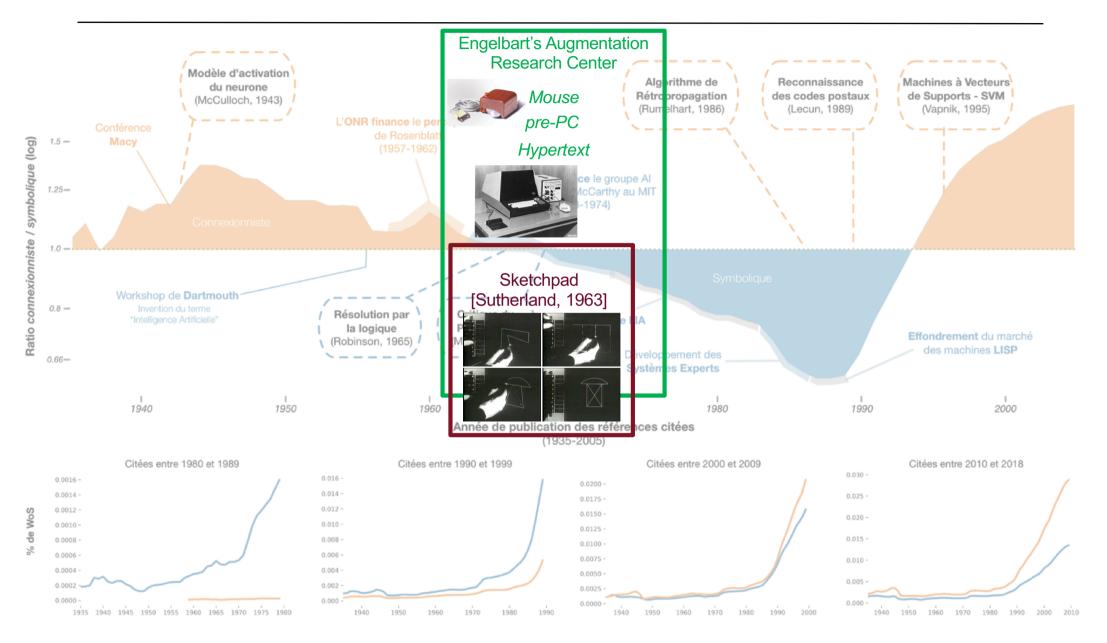
#### a research center for augmenting human intellect

This session is entirely devoted to a presentation by Dr. Engelbart on a computer-based, interactive, multiconsole display system which is being developed at Stanford Research Institute under the sponsorship of ARPA, NASA and RADC. The system is being used as an experimental laboratory for investigating principles by which interactive computer aids can augment intellectual capability. The techniques which are being described will, themselves, be used to augment the presentation.

The session will use an on-line, closed circuit television hook-up to the SRI computing system in Menlo Park. Following the presentation remote terminals to the system, in operation, may be viewed during the remainder of the conference in a special room set aside for that purpose.

https://web.stanford.edu/dept/SUL/library/extra4/sloan/MouseSite/1968Demo.html

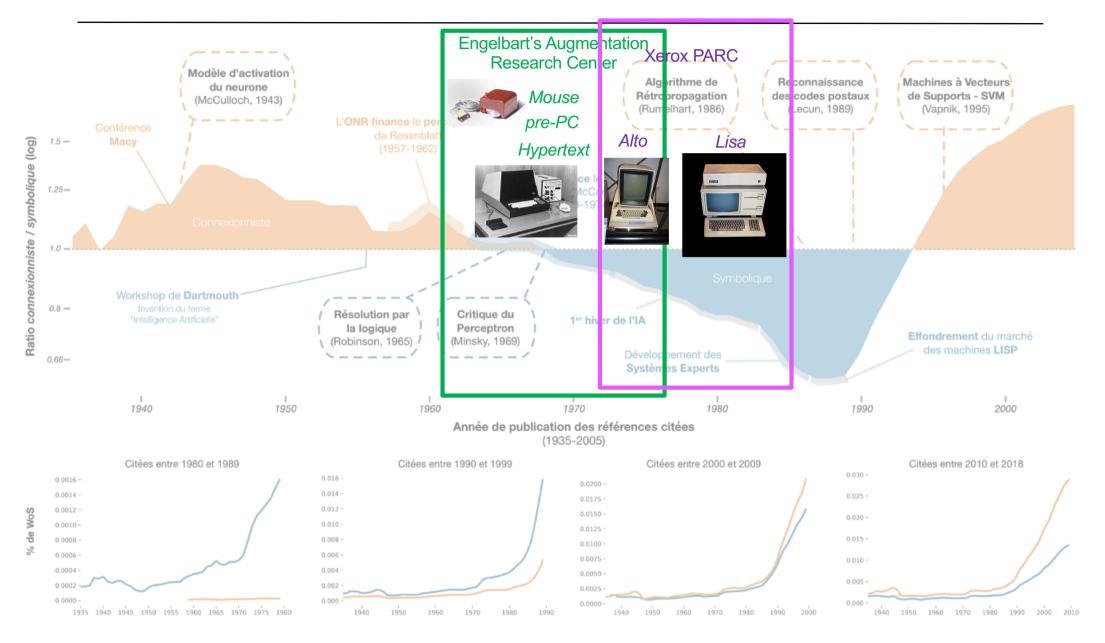
#### Al vs IA – History



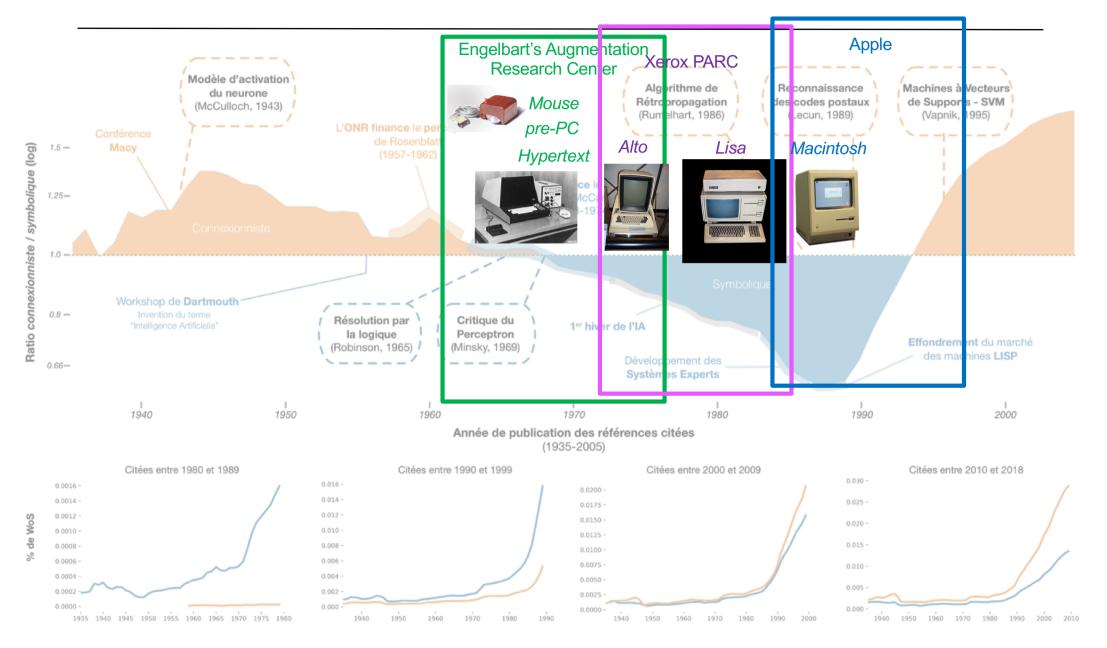
# Sketchpad [Sutherland, 1963]



#### Al vs IA – History



#### Al vs IA – History



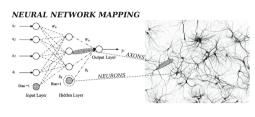
# Al and Connectionism with Progressive Incorporation of IA (Intelligence Augmentation & Interaction)

#### **Symbolic AI** [1956-]

Knowledge Representation Reasoning Planning



#### Connectionism [1957-]



Data Induction
Machine Learning
Pattern Recognition

#### Distributed AI [1975-]

Multi-Agent Systems Coordination Theory of Mind Active Learning [2009-]

Interactive User Query



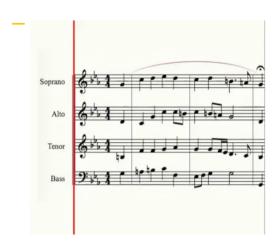
Personal Artificial Assistant [1990-] Software Agent

> Learning over User Shoulder Chatbot



#### **Autonomous vs Assistance Music Making**

- Autonomous Generation/Interpretation
  - Turing Test
  - Ambient Music





Compressorheads (no Al inside ©)

- Assistance to Human Composers and Musicians
  - Propose
  - Refine
  - Analyze
  - Harmonize
  - Produce
  - ...



#### **Various Open Issues**

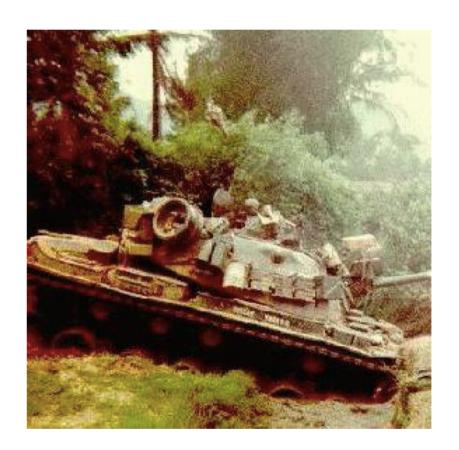
- Interpretability (Black Box)
- Reuse (Transfer Learning)
- Theory

• ...

# Pentagon Study, 1980

Automatic Classification Tank/no Tank Images





No Tank Tank

#### **Further Test**





Clear Sky Cloudy Sky

# **Missing Context**



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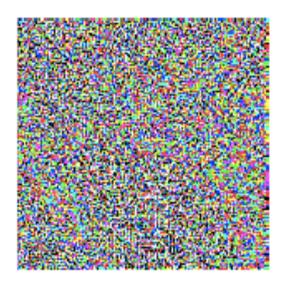
### **Missing Context**

https://www.scmp.com/tech/innovation/article/2174564/facial-recognition-catches-chinas-air-con-queen-dong-mingzhu

#### **Adversarial Neural Networks Generation**



 $+.007 \times$ 



 $\begin{array}{c} \epsilon \mathrm{sign}(\nabla_{\boldsymbol{x}} J(\boldsymbol{\theta}, \boldsymbol{x}, \boldsymbol{y})) \\ \text{"gibbon"} \end{array}$ 

 $\boldsymbol{x}$ "panda" 57.7% confidence

sign(
$$\nabla_{x}J(\theta, x, y)$$
)

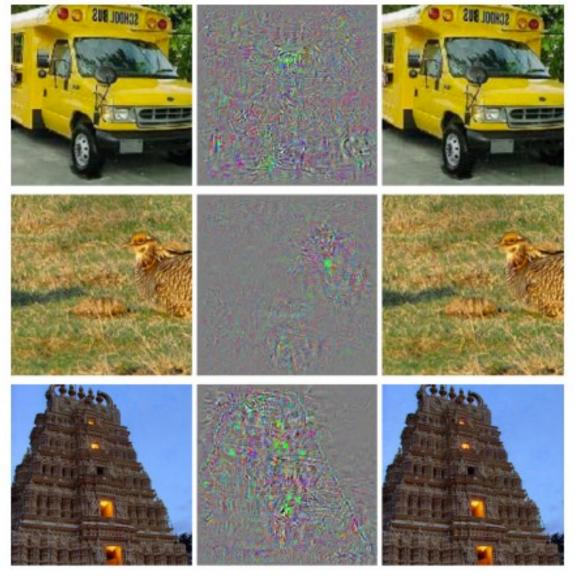
"nematode"

8.2% confidence

[Szegedy et al. 2014]

99.3 % confidence

#### **Adversarial Neural Networks Generation**



Correct class Perturbation Incorrect class
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[Szegedy et al. 2013]

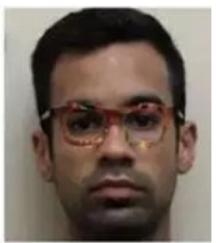
#### **Adversarial Neural Networks Glasses Generation**













#### Ex. of Handcrafted Features – Bag of Features [Brendel, 2019]

- Bag of Features (BoF) Model
- Define key Visual Features
  - Ex: Human eye, Feather





Count how often each Feature is Present in the Image



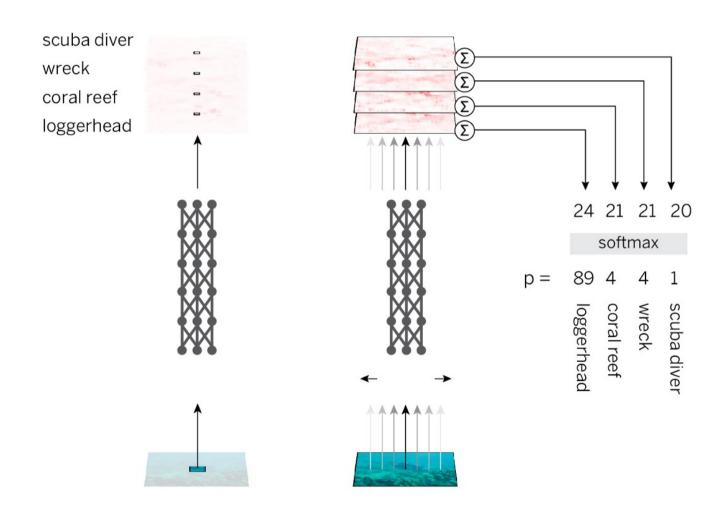


- Classify based on these Numbers
  - Human: Eye = 2
  - Bird: Feather = 18

# Bag of Feature Network (BagNet) [Brendel, 2019]

BagNets extract class activations (logits) on each patch Evaluating all patches yields one heatmap per class

Accumulating activations over space yields total class evidence



# Bag of Feature Network (BagNet) [Brendel, 2019]

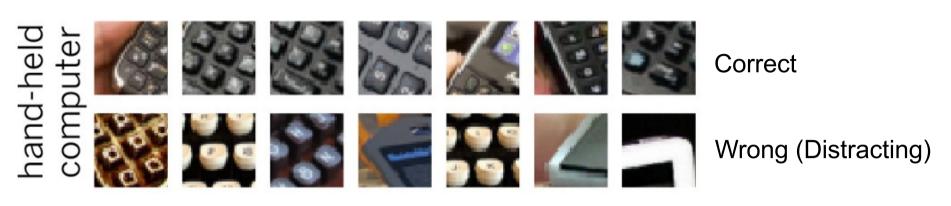
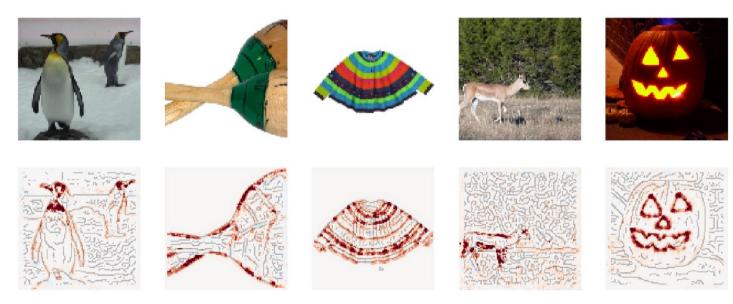


Image Features with most evidence



Heat maps (image parts which contributed most to decision)

### Feature Visualization and Activation Atlases [Olah et al., 2017]

- Based on DeepDream [Mordvintsev et al., 2015]
  - Iteratively adjust an image to maximize activation



- Visualizing Activations
  - Which pattern triggers activation







layer

 Helps to Analyze/Discriminate between Patterns and Correlations (e.g., stripes)

From One Neuron to Neuron Interactions
 & From One Example to Many Images (Next Slide)





Baseball—or stripes? mixed4a, Unit 6 133

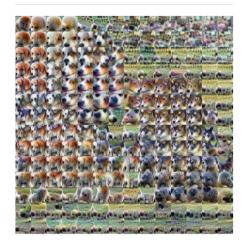
#### INDIVIDUAL NEURONS



#### **PAIRWISE INTERACTIONS**

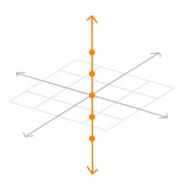


#### SPATIAL ACTIVATIONS

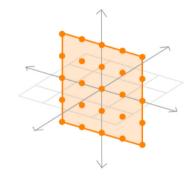


#### **ACTIVATION ATLAS**

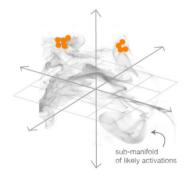




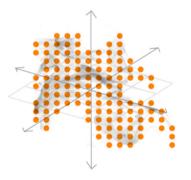
Visualizing individual neurons make hidden layers somewhat meaningful, but misses interactions between neurons — it only shows us one-dimensional, orthogonal probes of the high-dimensional activation space.



Pairwise interactions reveal interaction effects, but they only show two-dimensional slices of a space that has hundreds of dimensions, and many of the combinations are not realistic.

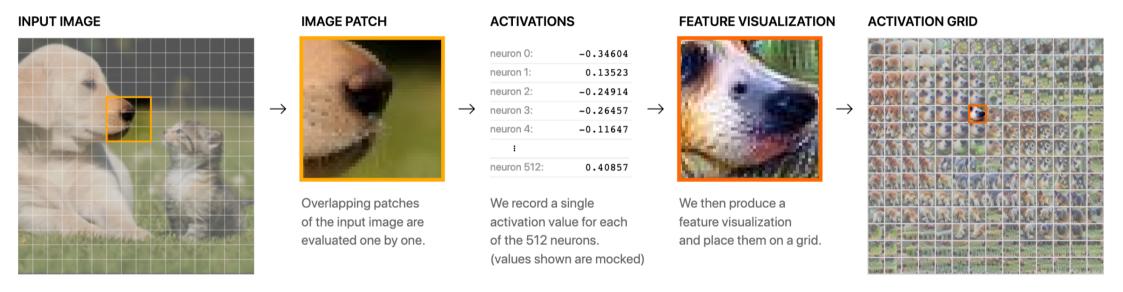


Spatial activations show us important combinations of many neurons by sampling the sub-manifold of likely activations, but they are limited to those that occur in the given example image.

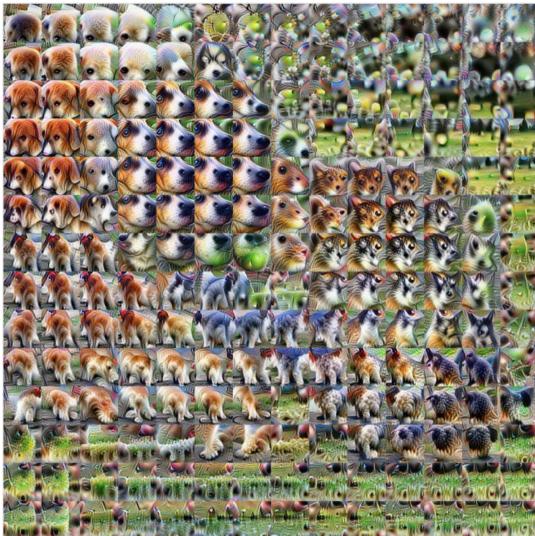


Activation atlases give us a bigger picture overview by sampling more of the manifold of likely activations.

- More details (interactive) in
  - https://distill.pub/2019/activation-atlas/

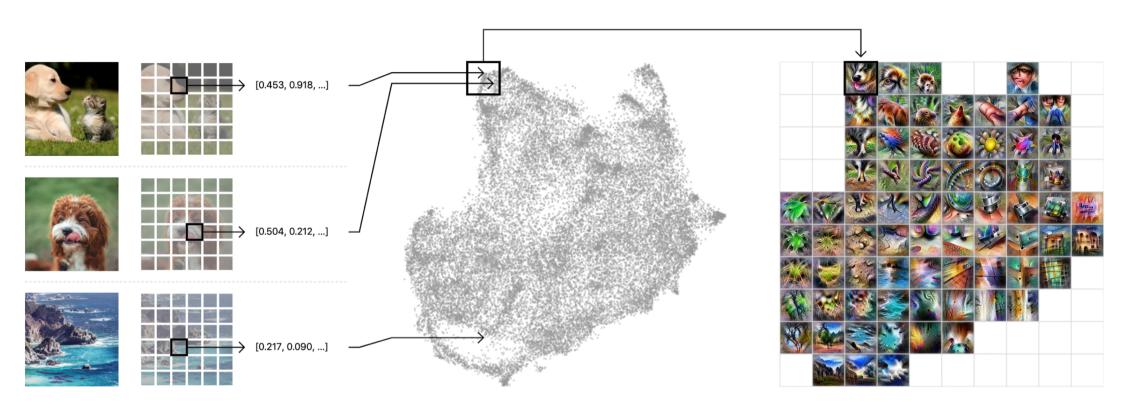






Input image from ImageNet.

Activation grid from InceptionV1, layer mixed4d.



A randomized set of one million images is fed through the network, collecting one random spatial activation per image. The activations are fed through UMAP to reduce them to two dimensions. They are then plotted, with similar activations placed near each other. We then draw a grid and average the activations that fall within a cell and run feature inversion on the averaged activation. We also optionally size the grid cells according to the density of the number of activations that are averaged within.



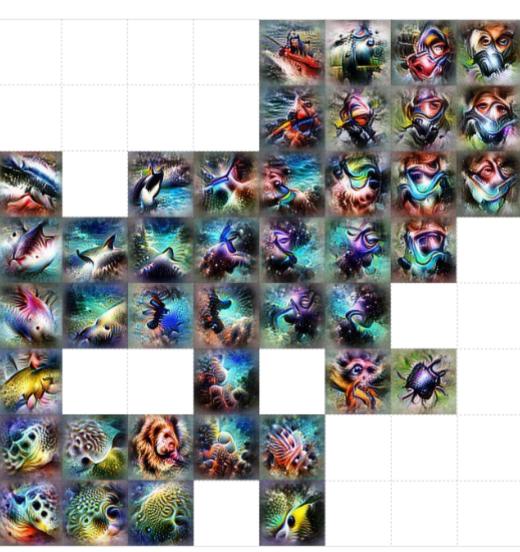


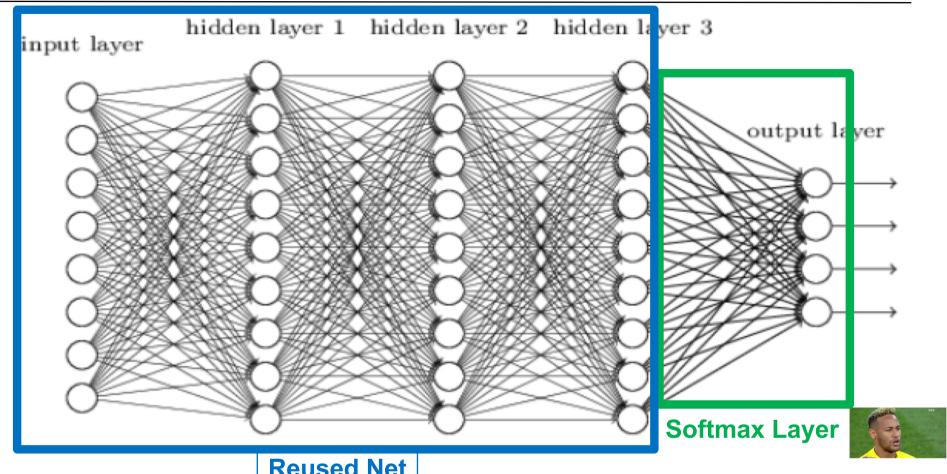




"SNORKEL" "SCUBA DIVER"



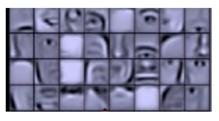




#### **Reused Net**







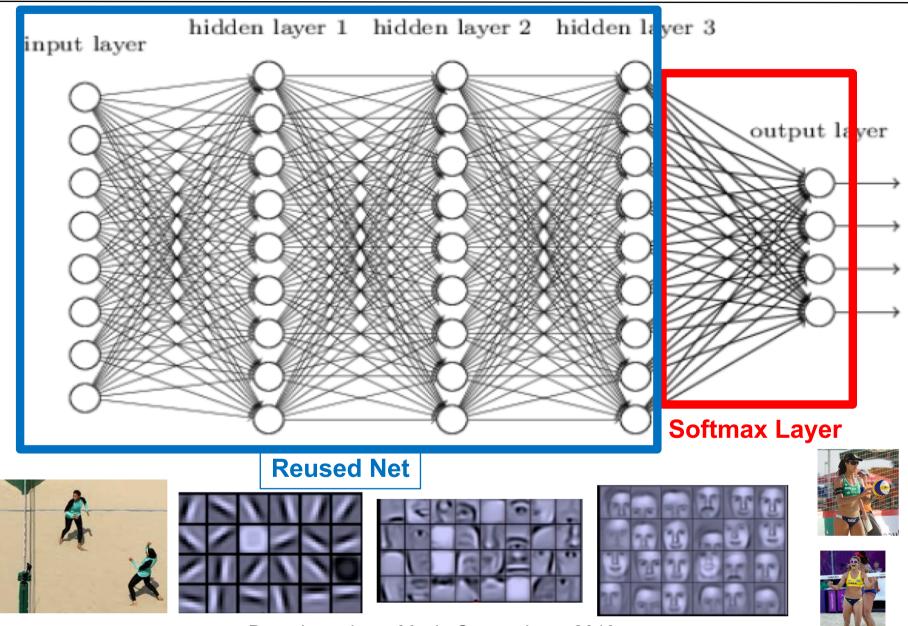






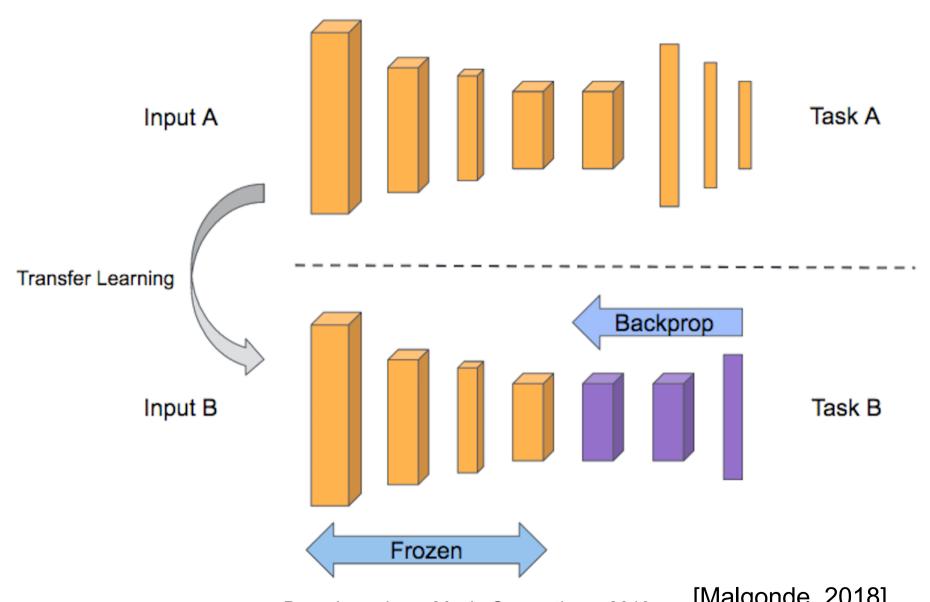
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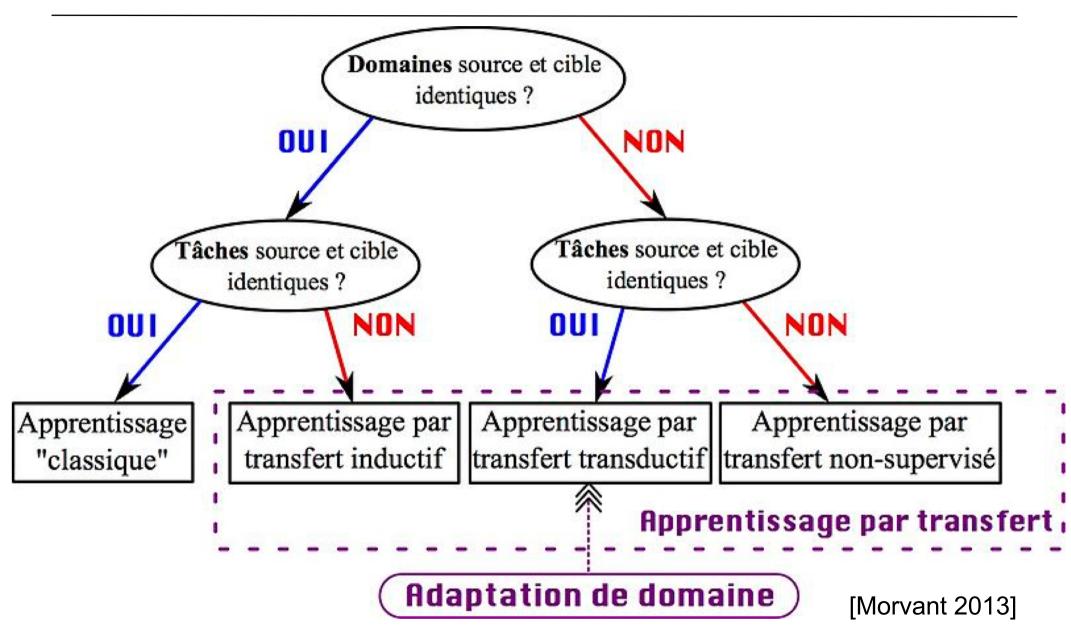
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#### Software Architecture View/issues of Deep Learning

- (Feedforward) Deep Network = Pipeline Hierarchical Architecture
- Software Components
  - Layers
  - Patterns (Convolutions, Conditioning...)
  - Hyper-Parameters
    - » Non Linear Operators/Modules: Sigmoid, Tanh, ReLU...
    - » Loss functions: Quadratic, Cross-entropy...
    - » Regularization: Weights-based, Dropout...
    - » Optimization: Batch Gradient descent, Stochastic Gradient, Branch and Bound...
    - » Initialization Algorithms

**—** ...

#### Software Engineering Issues

- Interoperability and Assemblage Assistance
  - » Frameworks
  - » Patterns and Anti-Patterns
- Substituability
  - » Type discipline (but Every data boils down to real numerical computation)
  - » Semantics
- Validation

#### **Limits**

- Specialized
- Data-based Model Generator
- Data-based (Statistical) Machine Learning only an (important) portion of Machine Learning
  - Reinforcement Learning
  - Inductive Logic Programming

**—** ...

- Machine Learning only an (important but small) portion of Artificial Intelligence
  - Reasoning
  - Planning
  - Knowledge Representation
  - User Modeling and Interaction
  - Collaboration (Multi-Agent Systems)
  - Natural Language Processing
  - Dialogue
  - Argumentation
  - Speech Processing
  - Decision
  - Game Theory
  - Optimization
  - Robotics

#### References

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  - https://www.coursera.org/learn/machine-learning
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  - http://www0.cs.ucl.ac.uk/staff/d.silver/web/Teaching.html
- L'apprentissage profond, Yann LeCun, Collège de France
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